# SCHEDULE OF MENTAL MATHS QUIZ COMPETITIONS FOR THE YEAR 2010-11 

| Practice to students from Question Banks | 01.04 .10 to 22.10 .10 |
| :--- | :--- |
| School level Quiz Competition | 23.10 .10 to 25.10 .10 |
| Cluster level Quiz Competition | 22.11 .10 to 25.11 .10 |
| Zonal level Quiz Competition | 01.12 .10 to 04.12.10 |
| District level Quiz Competition | 10.01 .11 to 12.01.11 |
| Regional level Quiz Competition | 14.01.11 to 15.01.11 |
| State level Quiz Competition | First week of February, 2011 |

State level Quiz Competition
First week of February, 2011


NAME OF THE TEACHER'S WHO REVIEWED THE QUESTION BANK FOR CLASS IX
S.No.
1.
2.
3. Neelam Kapoor
4. Vinti Singhla
5.

Rajesh Kr. Meena

Designation
Vice Principal
P.G.T.
P.G.T.
T.G.T.
T.G.T.

School
Govt. Co-ed. S. S. Maidangarhi, New Delhi. R.P.V.V. Tyagraj Nagar, Lodhi Road, N.D. - 03
Sister Nivedita, SKV, Defence Colony, A Block, New Delhi
Govt. Co-ed. S. S. Maidangarhi, New Delhi. Govt. Co-ed. S. S. Maidangarhi, New Delhi.

## Class - IX

## MATHEMATICS

INDEX
S. No. Chapter

1. Number System ..... 08
2. Polynomials ..... 13
3. Co-ordinate Geometry ..... 17
4. Linear Equations in two variables ..... 23
5. Introduction to Euclid's Geometry ..... 28
6. Lines and Angles ..... 33
7. Triangle ..... 43
8. Quadrilateral ..... 51
9. Circles ..... 57
10. Heron's Formula ..... 64
11. Surface Area and Formula ..... 67
12. Statistics ..... 70
13. Probability ..... 73

## CHAPTER-1 <br> Number System



$$
\begin{array}{|l}
\hline-,,-,-, \\
-,-3,-2,-1, \\
0,1,2,3,4, \\
-,,-, \\
-,-, \quad,
\end{array}
$$



1. Rational number is a number in the form of $p / q$, where p and q are integers and $q \quad 0$ Note that decimal representation of rational number is either terminating or non terminating but recurring.
2. A real number which is not a rational number is called an irrational number. Decimal
form of irrational number is neither terminating nor recurring. Thus, Real number = Rational numbers + Irrational numbers.
3. If $r$, is a rational number and $s$ is a irrational number, then their sum, $(r+s)$, difference $(r-s)$, products ( $r s$ ) and quotient ( $r / s$ ) are irrational numbers.
4. For positive real numbers a and $\mathrm{b}:-$
(i) $\sqrt{a b} \quad \sqrt{a} \cdot \sqrt{b}$
(ii) $\sqrt{\frac{a}{b}} \frac{\sqrt{a}}{\sqrt{b}}$
(iii) $\quad(\sqrt{a} \quad \sqrt{b})(\sqrt{a}-\sqrt{b}) \quad a-b$
(iv) $\quad(a \sqrt{b})(a-\sqrt{b}) \quad a^{2}-b$
(v) $\quad\left(\begin{array}{lllll}\sqrt{a} & \sqrt{b}\end{array}\right)^{2} \quad a \quad 2 \sqrt{a b} \quad b$
5. To rationalise the denominator of $\frac{1}{\sqrt{a} b}$, multiply this by $\frac{\sqrt{a}-b}{\sqrt{a}-b}$, where a and b are integers.
6. Laws of indices
(i) $a^{p} \cdot a^{q} \quad a^{p q}$
(ii) $a^{p^{q}} a^{p q}$
(iii) $\frac{a^{p}}{a^{q}} a^{p-q}$
(iv) $a^{p} b^{p} \quad(a b)^{p}$

Where, $a>0$ and a real number and $p$ and $q$ are rational numbers.

## CHAPTER-1 <br> Number System

1. Simplify $\sqrt[4]{32}$
2. Which is greater $\sqrt[3]{3}$ and $\sqrt[4]{5}$ ?
3. Write in ascending form $\sqrt[3]{4}, \sqrt[3]{2}, \sqrt[3]{3}$ ?
4. Simplify $\sqrt{8}+\sqrt{32}-\sqrt{2}$
5. Multiply $\sqrt[3]{7}$ by $\sqrt{2}$
6. Divide $\sqrt{24}$ by $\sqrt[3]{200}$
7. What is value of $\left(8^{3 / 5}\right)^{5}$ ?
8. What is value of $4^{1 / 5} 8^{1 / 5}$ ?
9. What is value of $8^{1 / 5} \div 8^{1 / 3}$ ?
10. Simplify $6^{3} \times\left(\frac{1}{2}\right)^{3}$
11. What is pure surd of $\frac{3}{4} \sqrt{32}$ ?
12. Write into simplest form $\sqrt[5]{3125}$
13. Simplify $4 \sqrt{3}+\sqrt{27}$
14. Find two rational numbers between $\frac{1}{2}$ and $\frac{1}{4}$
15. Find the two rational numbers between -1 and $\frac{3}{2}$
16. Find three rational numbers -5 and $\frac{3}{4}$
17. Find four rational numbers between -1 and 1
18. Express $\cdot \overline{37}$ in the form of $\frac{p}{q}$.
19. Express $\overline{54}$ in the form of $\frac{p}{q}$.
20. Express $3 . \overline{14}$ in the form of $\frac{p}{q}$.
21. What is the correct approximate decimal representation of $\sqrt{3}$ upto two decimals.
22. Express $\sqrt[3]{-108 a^{4} b^{3}}$ in the simplest form
23. Express $\sqrt[4]{a^{8} b^{6}} c^{7}$ in th simplest form.
24. What is the decimal representation of $3 \frac{3}{8}$.
25. What is the decimal representation of $\frac{5}{6}$.
26. Give the decimal representation of $\frac{327}{500}$.
27. Find three rational numbers between 0 and $\frac{1}{10}$.
28. What is the rational denominator of $\frac{1}{\sqrt{3}+\sqrt{2}}$
29. If $\sqrt{3}=1.732$, what is the value of $\frac{2}{\sqrt{3}}$.
30. Express $\frac{4}{\sqrt{5}-1}$ with rational denominator.
31. Express $\frac{10}{\sqrt{7}-\sqrt{5}}$ with rational denominator.
32. Express $\frac{16}{\sqrt{41}-5}$ with a rational denominator.
33. Find the value of $(512)^{\frac{-2}{9}}$.
34. Find the value of $(125)^{\frac{2}{9}}$
35. If $x=\sqrt{2}+1$, find the value of $\left(x-\frac{1}{x}\right)^{2}$.
36. Which of the following is rational or irrational number.
(i) $(2+\sqrt{3})^{2}$
(ii) $(3+\sqrt{4})^{2}$
37. If $P=3-2 \sqrt{2}$, what is the value of $P^{2}+\frac{1}{P^{2}}$.
38. Express as a pure Surd: $2 x y \sqrt[3]{x y}$.
39. Express as pure surd: $a^{\frac{1}{2}} \sqrt[3]{a b^{2}}$.
40. Find the value of $4 \sqrt{12} \times 7 \sqrt{6}$
41. Simplify $\sqrt{\frac{27}{80}}$.
42. Find the value of $\frac{1}{\sqrt{10}}$ when $\sqrt{10}=3.162$.
43. If $x=7+4 \sqrt{3}$, what is the value of $\sqrt{x}+\frac{1}{\sqrt{x}}$.
44. Find three rational numbers between 0 and 1 .
45. What is the value of $\frac{2+\sqrt{3}}{2-\sqrt{3}}$.
46. What is the value of $\frac{1}{3+\sqrt{2}}$ ?
47. Find the value of $\sqrt{8} \times \sqrt{50}$.
48. If $\sqrt{2}=1.41$, find the value of $\frac{1}{\sqrt{2}}$.
49. Divide $\sqrt{162}$ by $\sqrt{2}$.
50. Find the rationalising factor of $\sqrt[3]{49}$.
51. What is the value of $7 \sqrt{6} 5 \sqrt{24}$.
52. If $\sqrt{3}=1.732$, what is the value of $\frac{5}{\sqrt{3}}$ ?
53. If $\sqrt[3]{2}=(x)^{\frac{1}{2}}$, what is the value of $x$ ?
54. If $(\sqrt[4]{49})=x^{\frac{1}{2}}$, what is the value of $x$ ?
55. What is the value of $\begin{array}{lllll}3 \sqrt{5} & 2 \sqrt{3} & 3 \sqrt{5} & 2 \sqrt{3}\end{array}$ ?

## CHAPTER 1 <br> Answer <br> ( Number System )

1. $2 \sqrt[4]{2}$
2. $\sqrt[4]{5}$
3. $\quad \sqrt[3]{2}, \sqrt[3]{3}, \sqrt[3]{4}$
4. $\quad 5 \sqrt{2}$
5. $\sqrt[6]{392}$
6. $\sqrt[6]{\frac{216}{625}}$
7. 512
8. 2
9. $8^{-2 / 15}$ or $2^{-2 / 5}$
10. 27
11. $\sqrt{18}$
12. 5
13. $7 \sqrt{3}$
14. $3 / 8,7 / 16$
15. $\frac{-15}{16}, \frac{23}{16}$
16. $-17 / 8,-57 / 16, \frac{-45}{32}$
17. $0, \frac{-1}{2}, \frac{1}{2}, \frac{3}{4}$
18. $\frac{37}{99}$
19. $\frac{6}{11}$
20. $\frac{311}{99}$
21. 1.73
22. $-3 a b \sqrt[3]{4 a}$
23. $a^{2} b c \sqrt[4]{b^{2} c^{3}}$
24. 3.375
25. $0.8 \overline{3}$
26. 0.654
27. $1 / 40,1 / 20,3 / 40$
28. $\sqrt{3}-\sqrt{2}$
29. 1.154
30. $\sqrt{5}+1$
31. $5(\sqrt{7}+\sqrt{5})$
32. $\sqrt{41}+5$
33. $\frac{1}{4}$
34. $\sqrt[3]{25}$
35. 4
36. Irrational, rational
37. 34
38. $\sqrt[3]{8 x^{4} y^{4}}$
39. $\sqrt[3]{a^{5 / 2}} b^{2}$
40. $168 \sqrt{2}$
41. $\frac{3}{20} \sqrt{15}$
42. 0.316
43. 4
44. $\frac{1}{4}, \frac{1}{2}, \frac{3}{4}$
45. $7+4 \sqrt{3}$
46. $\frac{3-\sqrt{2}}{7}$
47. 20
48. . 705
49. 9
50. $\sqrt[3]{7}$
51. 420
52. 2.886
53. $\sqrt[3]{4}$
54. 7
55. 33

## CHAPTER-2

## Polynomials

All the algebric expressions having only whole numbers as the exponents of the variable. Such expressions in this form are called polynomials in one variable.

A polynomial of one term is called a monomial.

A polynomial of two terms is called a bionomial.

A polynomial of three terms is called a trinomial.

A polynomial of degree one is called a linear polynomial.

A polynomial of degree two is called a quadratic polynomial.

A polynomial of degree three is called a cubic polynomial.

A real number ' $a$ ' is a zero of a polynomial $p(x)$ if $p(a)=0$. In this case, $a$ is called also root of the equation $p(x)=0$

- The highest power of the variable in the polynomial is called degree of the polynomial.
- The degree of non zero constant polynomial is zero.

If $p(x)$ is any polynomial of degree greater then or equal to 1 and $p(x)$ is divided by the linear polynomial $(x-a)$, then the remainder is $p(a)$. This is called Remainder Theorem.

If $x-a$ is a factor of the polynomial $p(x)$, then $p(a)=0$. This is known as Factor Theorem.
(i) $\quad\left(\begin{array}{lllllllll}x & y & z\end{array}\right)^{2} \quad x^{2} \quad y^{2} \quad z^{2} \quad 2 x y \quad 2 y z \quad 2 z x$
(ii) $\left.\quad \begin{array}{llllll}x & y\end{array}\right)^{3} \quad x^{3} \quad y^{3} 3 x y\left(\begin{array}{ll}x & y\end{array}\right)$
(iii) $\quad(x-y)^{3} x^{3}-y^{3}-3 x y(x-y)$
(iv) $\quad x^{3}-y^{3} \quad(x-y)\left[\begin{array}{lll}(x-y)^{2} & 3 x y\end{array}\right] \quad(x-y)\left(\begin{array}{lll}x^{2} & x y & y^{2}\end{array}\right)$
(v) $\quad x^{3} \quad y^{3} \quad\left(\begin{array}{ll}x & y\end{array}\right)\left[\left(\begin{array}{ll}x & y\end{array}\right)^{2}-3 x y\right] \quad\left(\begin{array}{ll}x & y\end{array}\right)\left(x^{2}-x y \quad y^{2}\right)$
(vi) If, $a+b+c=0$, then $a^{3}+b^{3}+c^{3}=3 a b c$
(vii) $\quad x^{2} \frac{1}{x^{2}} \quad x-\frac{1}{x}^{2} \quad 2$
(viii) $\quad x^{2} \quad \frac{1}{x^{2}} \quad x \quad \frac{1}{x}{ }^{2}-2$
(ix) $\begin{array}{lllllll}x^{2} & y^{2} & z^{2} & \left(\begin{array}{lll}x & y & z\end{array}\right)^{2}-2\left(\begin{array}{lll}x y & y z & z x\end{array}\right)\end{array}$

$$
\begin{array}{rlllllll}
x^{3} & y^{3} & z^{3}-3 x y z & \left(\begin{array}{llll}
x & y & z
\end{array}\right)\left(\begin{array}{lll}
x^{2} & y^{2} & z^{2}-x y-y z-z x
\end{array}\right. \\
& \left(\begin{array}{llllll}
x & y & z
\end{array}\right)\left\{\left(\begin{array}{llll}
x & y & z
\end{array}\right)^{2}-3\left(\begin{array}{lll}
x y & y z & z x
\end{array}\right)\right.
\end{array}
$$

(x) $\quad x^{3}-\frac{1}{x^{3}} \quad x-\frac{1}{x} \quad x-\frac{1}{x}^{2} \quad 3$
(xi) $\quad x^{3} \frac{1}{x^{3}} \quad x \quad \frac{1}{x} \quad x \quad \frac{1}{x}^{2}-3$
(xii) $\quad x^{4} \quad \frac{1}{x^{4}} \quad x^{2} \quad \frac{1}{x^{2}} \quad{ }^{2}-2$
(xiii) $\sqrt{x} \frac{1}{\sqrt{x}} \sqrt{x \frac{1}{x} \quad 2}$
(xiv) $\sqrt{x}-\frac{1}{\sqrt{x}} \sqrt{x \frac{1}{x}-2}$

## CHAPTER-2

## Polynomials

1. What is the degree of the polynomial $4-y^{2}$ ?
2. What is the degree of the polynomial $5 x^{3}+4 x^{2}+7 x$ ?
3. Whether the following polynomials are linear, quadratic or cubic polynomials.
(i) $x-x^{3}$
(ii) $y+y^{2}+4$
(iii) $3 t$
4. What is the value of the polynomial $-4 x^{2}+7 x-5$ when $x=-3$ ?
5. If $f(x)=2 x^{3}-3 x^{2}+12$ then find $f(2)$.
6. What is the degree of the polynomial $\left(y^{3}-2\right)\left(y^{2}+11\right)$.
7. If $\mathrm{P}(\mathrm{y})=y^{2}-y+1$ then what is value of $\mathrm{P}(3)$.
8. What is the zero of the polynomial $P(x)=x+5$ ?
9. What is the Coefficient of x in the expression $\frac{x}{2}+y+Z$ ?
10. What is the Coefficient of $x$ in the expression $x^{2} \sqrt{5} x \quad 2$ ?
11. What is the degree of the polynomial 20 ?
12. What is the standard form of $y^{2}+6 y+9+4 y^{4}$ ?
13. What is the standard form of $q^{2}+4 q^{8}-q^{6}$ ?
14. What is the remainder when $\mathrm{p}(\mathrm{x})=x^{3}-a x^{2}+6 x-a$ is divided by $\mathrm{x}-\mathrm{a}$ ?
15. Find the remainder when $x^{51}+51$ is divided by $x+1$.
16. Find the value of K if $\mathrm{x}+3$ is a factor of $3 x^{2}+k x+6$.
17. Express $8 x^{3}+60 x^{2}+150 x+125$ as a cube of binomial.
18. Factorize $9 p^{2}-16 q^{2}$.
19. Facrorize $x\left(x^{2}+y^{2}-z^{2}\right)-z\left(x^{2}+y^{2}-z^{2}\right)$.
20. Expand $(x+5 y)^{3}$.
21. Expand $(2 x-7)^{3}$.
22. Expand $(3 x-1)^{2}$.
23. Expand $(x+2)^{2}$.
24. Factorize $50 x^{2}-72 y^{2}$.
25. Factorize $m^{2}+2 \sqrt{3} m+3$.
26. Find the zeros of polynomials $x^{2}+14 x+40$.
27. What is the product of Zero's of polynomials $(x+8)(x-10)$.
28. Facroeize $9 x^{2}-\frac{y^{2}}{100}$
29. What is the degree of polynomial $4 y^{2}-4 y+1$.
30. Factorize $8 a^{3}-b^{3}-12 a^{2} b+6 a b^{2}$.
31. Factorize $8 x^{3}+27 y^{3}+36 x^{2} y+54 x y^{2}$
32. Factorize $36 a^{2}+60 a b+25 b^{2}$.
33. Find the product $(x-5)(x+4)$.
34. Find the product $(x-3)(x-7)$.
35. Find the product $(x+6)(x+8)$.
36. Find the remainder when $p(x)=x^{3}+x^{2}+x+1$ is divided by $g(x)=x+1$.
37. If $\mathrm{p}(\mathrm{x})=\mathrm{x}^{4}+3 x^{3}+3 x^{2}+x+1$ and $\mathrm{g}(\mathrm{x})=\mathrm{x}+1$ then find the remainder when $\mathrm{p}(\mathrm{x})$ is divided by $g(x)$.
38. Find the value of $K$ if $x-2$ is the factor of $x^{3}-2 x^{2}-x+k$.
39. Find the value of K if $x+1$ is the factor of $x^{3}-k x^{2}-9 x-5$.
40. Find the value of K if $\mathrm{x}-1$ is factor of $3 x^{4}-k x^{3}-3 x+4$.
41. Find the value of K if $\mathrm{x}+1$ is facror of $3 x^{2}+x+k$.
42. What is the Coefficient of $x^{2}$ in the polynomial $3 x^{3}-15 x^{2}+10 x-2$.
43. Find the value of $p(x)=x^{2}-4 x+7$ when $x=3$.
44. Find the value of $\mathrm{f}\left(\frac{-3}{2}\right)$ when $\mathrm{f}(\mathrm{x})=4 x^{2}+3 x+\frac{7}{2}$.
45. If $f(x)=x^{2}-5 x-14$ find the value of $f(7)$.
46. Find the zeros of the polynomial $x^{2}-15 x-34$.
47. What should be added to the polynomial $x^{2} \quad 5 x \quad 4 x$. so that 3 is a zero of the polynomial.
48. Which of the number $3,2,-2,1$ are zeros of the polynomial $x^{2}-4$ ?
49. Find the quotient when $x^{2}-7 x+12$ is divided by $(x-3)$.
50. Find the polynomial whose zeros are $\sqrt{2}$ and $-\sqrt{2}$.

## CHAPTER 2 <br> Answer <br> ( Polynomials )

1. 2
2. 3
3. (i) Cubic (ii) Quadratic
(iii) linear
4. -62
5. 16
6. 5
7. 7
8. -5
9. $\frac{1}{2}$
10. $-\sqrt{5}$
11. zero
12. $4 y^{4}+y^{2}+6 y+9$
13. $4 q^{8}-q^{6}+q^{2}$
14. 5 a
15. 50
16. 11
17. $(2 x+5)^{3}$
18. $(3 p+4 q)(3 p-4 q)$
19. $(x-z)\left(x^{2}+y^{2}-z^{2}\right)$
20. $x^{3}+125 y^{3}+15 x^{2} y+75 x y^{2}$
21. $8 x^{3}-343-84 x^{2}+294 x$
22. $9 x^{2}-6 x+1$
23. $x^{2}+4 x+4$
24. $2(5 x+6 y)(5 x-6 y)$
25. $(m+\sqrt{3})^{2}$
26. $(-4,-10)$
27. -80
28. $\left(3 x+\frac{y}{10}\right)\left(3 x-\frac{y}{10}\right)$
29. 2
30. $(2 a-b)^{3}$
31. $(2 x+3 y)^{3}$
32. $(6 a+5 b)^{2}$
33. $x^{2}-x-20$
34. $x^{2}-10 x+21$
35. $x^{2}+14 x+48$
36. 0
37. $k=2$
38. $k=3$
39. $k=4$
40. -15
41. 8
42. $17,-2$
43. $2,-2$
44. $x^{2}-2$

## CHAPTER-3

## Co-ordinate Geometry

- To locate the position of an object or a point in a plane, we require two prependicular lines. One of them is horizontal and the other is vertial.
- The plane is called the cartesian or coordinate plane.
- The horizontal line is called the x-axis, and the vertical line is called the y-axis.

- The x and y axis divide the plane into four parts called quadrants.
- The point of intersection of the axis is called the origin.
- The distance of the point from the $y$-axis is called its x-coordinate, or abscissa, and the distance of the point from the $x$-axis is called its $y$-coordinate or ordinate.
- The coordinates of a point on the $x$-axis are of the form ( $\mathrm{x}, 0$ ) and that of the point on the $y$-axis are ( $0, y$ )
- The coordinates of the origin are $(0,0)$
- The coordinates of a point in quadrants :-
(i) I Quadrant (+,+)
(ii) II Quadrant (-,+)
(iii) III Quadrant (-,-)
(iv) IV Quadrant (+,-)
where, + denotes a positive real number and - denotes a negetive real number.

The equation of $x$-axis is $y=0$.

The equation of y -axis is $\mathrm{x}=0$.

If, ( $\left.\begin{array}{ll}x & y\end{array}\right)$
then $(x, y) \quad(y, x)$
and if $x=y$ then
$(x, y)=(y, x)$

## CHAPTER-3

## Co-ordinate Geometry

1. Name the mathematician who developed Co-ordinate geometry.
2. How many points are required to locate a line segment?
3. The axis divide the plane into four parts. What these four parts called?
4. What are the co-ordinates of origin?
5. What is the point of intersection of axis called?
6. What is the distance of a point form $y$-axis called?
7. What is the distance of a point from $x$-axis called?
8. What is the name of the horizontal and vertical lines drawn to determine the position of any point to the cartesian plane?
9. What is the equation of $x$-axis?
10. Line $y=0$ represents which axis?
11. Line $y=2$ is parallel to which axis?
12. Line $x=-3$ is parallel to which axis?
13. What is the perpendicular distance of the point $P(4,3)$ from $x$-axis?
14. What is the perpendicular distance of the point $Q(5,7)$ from $y$-axis?
15. Which of the following points lie in the fourth quadrant $(-3,-5),(2,-1),(-2,4),(4,-7)$, $(5,6)$ ?
16. Name the figure obtained by joining the points $(0,0),(5,0),(5,5),(0,5)$ in the cartesian plane.
17. Name the figure obtained by joining the points $(0,0),(5,0),(5,3)$ and $(0,3)$ in the cartesian plane.
18. Name the figure obtained by joining the points $(-5,0),(0,5)$ and $(5,0)$ in the cartesian plane.
19. Name the axis on which the point $(7,0)$ lie.
20. Name the axis on which the point $(0,9)$ lie.
21. Find the co-ordinates of the point whose abscissa is 9 and ordinate is -2 .
22. Find the co-ordinates of the point whose ordianate is 3 and lies on $x$ - axis.
23. Find the co-ordinates of the point whose abscissa is -3 and lies on $x$ - axis..
24. Name the quadrant in which the point $(-2,4)$ lies.
25. If the points $P(1,0), Q(5,0), R(5,2)$ and $S$ forms a rectangle. Then find the fourth vertex S .
26. If the points $A(0,0), B(2,0), C(2,2)$ are three vertices of a square then find the fourth vertex of the square.
27. Which of the following points lie on $x$-axis
(i) $(3,0)$
(ii) $(2,-3)$
28. If the point $(x, y)$ lies on $x$-axis then what is the value of $y$ ?
29. If the point $(x, y)$ lies on $y$-axis then what is the value of $x$ ?
30. Find the co-ordinate of the point whose abscissa is $\frac{9}{2}$ and ordinate is 5 .
31. Find the co-ordinate of the point whose abscissa is 3and ordinate is $\frac{7}{2}$.
32. Which of the following point lies on $x$-axis.
(i) $(0,-2)$
(ii) $(-2,0)$
33. Which of the following point lies on y-axis.
(i) $(0,-3)$
(II) $(2,-3)$
34. Which of the following point lies on x-axis.
(i) $(0,0)$
(II) $(5,0)$
35. A point lies on $x$-axis at a distance of 6 units from $y$-axis and lies on right side of origin. Find the co-ordinates of the point..
36. A point lies on $y$-axis at a distance of 1 units from $x$-axis and lies above $x$-axis. Find the co-ordinates of the point..

37 Write down the co-ordinates of point $A, B, C, D$

38. Write down the co-ordinates of point $A, B, C, D, E, F, G$ and $H$.


40. In the figure what is the perpendicular distance of the point $P$ from the $y$ axis measured along the positive direction of x axis.
41. In the figure what is the perpendicular distance of the point $P$ from the $x$ axis measured along the positive direction of $y$ axis.


42. In the given figure find
(i) The co-ordinates of A
(ii) The co-ordinates of B
(iii) The co-ordinates of C
(iv) The co-ordinates of $D$
43.



In the given figure find
(i) The ordinate of the point H
(ii) The ordinate of the point I.
44. In the given figure find
(i) The abscissa of the point D
(ii) The abscissa of the point E
45. In the given figure find
(i) The Point identified by the co-ordinate of $(-2,-3)$
(ii) The Point identified by the co-ordinate of $(3,-3)$.


46. In the given figure find
(i) The co-ordinate of the point L
(ii) The co-ordinate of the point M

47. Name the quadrant in which the following points lie?
(i) $(-7,-5)$
(ii) $(2,-9)$
(iii) $(9,0)$
(iv) $(0,5)$

## CHAPTER 3 <br> Answer <br> ( Co-ordinate Geometry)

1. Rene Descrete
2. Two
3. Quadrants
4. $(0,0)$
5. Origin
6. Abscissa
7. Ordinate
8. $x$-axis and $y$-axis
9. $y=0$
10. $x$ - axis
11. x - axis
12. $y-a x i s$
13. 3 units
14. 5 units
15. $(2,-1) \&(4,-7)$
16. Square
17. Rectangle
18. Traingle
19. $x$ - axis
20. $y$-axis
21. $(9,-2)$
22. $(0,3)$
23. $(-3,0)$
24. II quadrant
25. $(1,2)$
26. (0, 2)
27. $(3,0)$
28. $y=0$
29. $x=0$
30. $(4.5,5)$
31. $(3,3.5)$
32. $(-2,0)$
33. ( $0,-3$ )
34. $(5,0)$
35. (6, O)
36. $(0,1)$
37. $A(6,2), B(4,-4), C(-5,2), D(-3,-4)$
$38 \quad \mathrm{~A}(2,3), \mathrm{B}(-4,2), \mathrm{C}(-5,-3), \mathrm{D}(5,-2)$, $E(2,-4), F(3,0), G(-2,0), H(0,4)$
38. Traingle $B(-4,4) A(4,4), C(0,0)$
39. X-co-ordinate or abscissa
40. Y-co-ordinate or ordinate
41. $A(2,2), B(-3,0), C(-2,-4), D(3,-1)$
42. (i) -2 , (ii) 3
43. (i) 5
(ii) 4
44. (i) E (ii) D
45. $\mathrm{L}(1,2)$ (ii) $\mathrm{M}(-1,-2)$
46. (i) $3^{\text {rd }}$ Quadrant
(ii) $4^{\text {th }}$ Quadrant
(iii) $x$-axis
(iv) $y$-axis

## CHAPTER-4 <br> Linear Equation in Two Variable

An equation of the form $a x+b y+c=0$, where $a, b$ and $c$ are real numbers, such that $a$ and $b$ are not both zero, is called a linear equation in two variables.

A linear equation in two variables has infinitely many solutions.

- The graph of every linear equations in two variables is a straight line.
- The graph of $x=a$ is a straight line parallel to the $y$-axis.
- The graph of $y=a$ is a straight line parallel to the $x$-axis
- Every solution to the linear equation is a point on the graph of the linear equation.


## CHAPTER-4

## Linear Equation in Two Variable

1. What is an equation?
2. What is a linear equation in one variable?
3. How many solutions does a linear equation in one variable has?
4. What is a linear equation in two variables?
5. How many solutions does a linear equation in two variables have?
6. What is the value of $y$ in terms of $x$.
$a x+b y+c=0, \quad(a \neq 0, b \neq 0)$
7. What is the $y$-form of the equation $x-2 y=4$.
8. What is the $x$-form of the equation $2 x+5 y=9$.
9. What is the $x$-form of the equation $\pi x+y=9$.
10. Compare the linear equation $3 x \quad 8 \quad \sqrt{2} y$ with $a x+b y+C=0$ and indicate the values of $a, b$ and $c$.
11. Compare $2 x=-6 y$ with $a x+b y+C=0$, and indicate the values of $a, b$ and $c$.
12. Express $x-\frac{y}{5}-10=0$ in the form of $a x+b y+C=0$, and indicate the values of $\mathrm{a}, \mathrm{b}$ and c.
13. Express $x=-9$ as a linear equation in two variables.
14. Express $3 y=7$ as a linear equation in two variables.
15. Express $5 y=2$ as a linear equation in two variables.
16. Find whether $x=2, y=1$ is a solution of a linear equation $5 x+3 y=14$.
17. Verify whether $x=12$ is a solution of the eqution $0.5 x+\frac{x}{3}=0.25 x+9$.
18. Examine if $x=0$ is a solution of the equation $(x-2)+(x+3)=x+8$.
19. Verify if $x=2$ is a solution of the equation $\frac{3 x-1}{4}+\frac{3}{4}=2$.
20. Examine if 3 is a solution of $x-7=3 x+8$.
21. Find the coordinates of the points where the equation $3 x+y=6$ intersects both the axis.
22. Find the coordinates of the points where the equation $y-3 x=9$ intersects both the axis.
23. Does the point $(4,1)$ lies on the equation $2 x+5 y=13$ ?
24. Find the coordinates of the points where the equation $2 x-3 y=6$ intersects $x$-axis and $y$-axis.
25. Find any two solutions for the following linear equations in two variables:
(i) $2 x+5 y=13$
(ii) $x+y+4=0$
(iii) $(x-4)-y+4=0$

Find the value of ' $p$ ' so that the following equations may have $x=1, y=1$ as a solution: (26) $3 x+p y=6$
(27) $p x-2 y=10$
(28) $5 x+2 p y=3 a$

Represent the given statements as a linear equations in two variables.
29. A number is $\frac{2}{3}$ of the other number.
30. The sum of the ages of a brother and a sister is 50 years.
31. Rupali is 7 times as old as Jayana.
32. Two times of a number when added to another number gives 15.
33. Choose the correct equation from the choices given for the following graph:
(i) $y=x$
(ii) $x+y=0$
(iii) $y=2 x$
(iv) $2+3 y=7 x$

34. Observe the graph and give the corresponding equations for it.

35. Observe the graph and give the corresponding equations

36. To which axis the graph of the equation $3 x-2=0$ is parallel.
37. To which axis the graph of the equation $y=-5$ is a line parallel.
38. At which point the graph of the equation $x=-3$ intersects $x$-axis?.
39. At which point the graph of the equation $x+y=0$ intersect $x$-axis and $y$-axis?
40. Which axis does $\mathrm{y}=0$ represents?
41. In the graph $y=2$ what will be the ordinate for any value of abscissa.
42. In the graph $x=-1$ what will be the ordinate for any value of abscissa.
43. To which axis the graph of $x=-1$ will be parallel to?
44. How many solutions a linear equation in two variables have?
45. The auto fare in Delhi is as follows: For the first kilometer, the fare of Rs. 10 and for each subsequent distance it is Rs. 5 per km. If the distance covered is $x \mathrm{~km}$ and the total fare is Rs. y. Represnt this information as a Linear Equation.
46. A pen costs Rs. 10 and a pencil costs Rs. 2. Form an equation that represents the total money spent on buying different combinations of pen and pencils, if the total money spent is Rs. 110.
47. Verify that which among the following is not a solution of equation $2 x-y=4$
(i) $x=0, y=-4$
(ii) $x=3, y=2$
(iii) $x=1, y=1$
(iv) $y=0, x=2$
48. Represent $3 x+5 y-11=0$ as $y$ in the form of $x$. Find the point where the equation intersects $y$-axis.

## CHAPTER 4

Answer

## ( Linear Equation in Two Variable )

1. An equation is a statement of equality involving one or more unknown quant ities called variable.
2. An equation is called a linear equa tion in one variable, if only a single variable with degree one occurs in the equation.
3. Only one solution
4. A linear equation in the form of $a x+$ by $+\mathrm{c}=0$ wher $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are real num bers, $a \neq 0, b \neq 0$, and $x$ and $y$ are two variables.
5. Infinite solutions.
6. $y=\frac{-c-a x}{b}$
7. $y=\frac{x-4}{2}$
8. $x=\frac{9-5 y}{2}$
9. $x=\frac{9-y}{\pi}$
10. $a=3, b=-\sqrt{2}, c=-8$
11. $a=2, b=6, c=0$
12. $5 x-y-50=0, a=5, b=-1, c=-50$
13. $x-0 y+9=0$
14. $0 x+3 y-7=0$
15. $0 x+5 y-2=0$
16. No
17. No
18. No
19. Yes
20. No
21. $(2,0)(0,6)$
22. on x-axis $(-3,0)$, on $y$-axis $(0,9)$
23. Yes
24. $x$-axis $(3,0), y$-axis - $(0,-2)$
25. (i) $(4,1) \quad\left(\frac{1}{2}, \frac{12}{5}\right)$
(ii) $(-2,-2)(1,-5)$
(iii) $(1,1)(2,2)$
26. $p=3$
27. $p=12$
28. $p=\frac{3 a-5}{2}$
29. $x=\frac{2}{3} y$
30. $x+y=50$
31. $x=7 y$
32. $2 x+y=15$
33. (ii) $x+y=0$
34. $x=2$
35. $y=1$
36. $y$-axis
37. $x$-axis
38. $(-3,0)$
39. $(0,0)$
40. $x$ - axis
41. $y=2$
42. $y$-axis
43. $y$-axis
44. Infinite solution
45. $y=5(x-1)+10 \Rightarrow y=5 x+5$
46. $10 x+2 y=110$, where $x=$ no. of pens bought $y=$ no. of pencils boughts.
47. III is not the solution.
48. $y \frac{11-3 x}{5}$, point is $\left(0, \frac{11}{5}\right)$

## CHAPTER-5

## Introduction to Euclid's Geometry

1. Which are the two greek words, the word 'geomentry' has been derived from?
2. What is the meaning of these two words?
3. What does the word 'geometry' mean?
4. Who were the first people to study geometry?
5. Who were the people who used the knowledge of geomentry for calculating areas of fields and volume of grain storehouses.
6. Who developed formulae for areas of rectilinear figures such as rectangles and traiangles.
7. To whom goes the credit for the systematic study of geometry.
8. Name the two most well known greek Mathematicians?
9. Who is known as the 'father of geometry'?
10. What is the name of Euclid's most famous work?
11. Name two Indian mathematicians who contributed significantly in the field of geometry?
12. What is the difference between axioms and postulates?
13. State Euclid's postulate for a straight line.
14. State Euclid's postulate for a straight circle.
15. What is Euclid's postulate on right angles?
16. What is Euclid's fifth postulate ?
17. Who restated the fifth postulate of Euclid's?
18. What is the name given to restated form of Euclid's fifth postulate?
19. Give the statement of restated form of Euclid's fifth postulate?
20. What is the difference between axioms and Theorems?
21. What is the historical importance of Euclid's fifth postulate?
22. What is the least number of distinct points which determine a unique line?
23. In how many maximum numbers of points can two distinct lines intersect?
24. State playfair's Axiom.
25. What is the name of the work that contained Euclid's thirteen volumes?
26. How many lines can be drawn through a single point?
27. Can two distinct intersecting lines be parallel to the same line? Why?
28. Given two points $L$ and $M$, how many line segments do they determine?
29. Name the line segments determined by three collinear points $x, y$ and $z$ ?
30. What are the three basic concepts in geometry?

Fill in the blanks: Q. No. 31 to Q. No. 37.
31. Things which are equal to the same things are $\qquad$ to one another.
32. The $\qquad$ is greater than the part.
33. Things which are double of the $\qquad$ are equal to one another.
34. Two distinct point in a plane determine a $\qquad$ line.
35. A line seperates a plane into $\qquad$ parts namely the $\qquad$ and the
$\qquad$ itself.
36. Two distinct $\qquad$ in a plane cannot have more than one point in common.
37. Given line and a point, not on the line, there is one and only one $\qquad$ line which passes through the given point and is $\qquad$ to the line.
38. If $B$ lies between $A$ and $C, A C=15 \mathrm{~cm}, B C=9 \mathrm{~cm}$, what is $(A B)^{2}$
39. Does a line have any length.
40. Give an example of geometrical straight line.
41. In fig 1 name the following
(i) 3 line segments
(ii) 4 collinear points
(iii) a pair of non-intersecting line segments.

42. What is the difference between intersecting lines and concurrent lines?
43. State parallel Axiom.
44. If line $A B, A C, A D, A R$ are parallel to a line $I$, then points $A, B, C, D$ and $R$ are
$\qquad$ -.
45. What do you understand 'betweenness'?
46. Explain mid point of a line segment with the help of an example.
47. Explain congruence of line segments.
48. Give the definition of the point as given by Euclid.
49. Give the definition of a 'line' as given by Euclid.
50. With reference to the fig 2 given below, state which statement is true and which is false.

(i) $P Q+Q R=P R$
(ii) $\mathrm{PR}+\mathrm{PS}=\mathrm{PS}$
(iii) Lines PQ and PS are coincident.
(iv) Points R, S, T lie on the line PQ.

## CHAPTER 5 <br> Answer <br> ( Introduction to Euclid's Geometry )

1. 'geo' and 'metrien'
2. 'Geo' means 'the earth' 'metrien' meand 'measure'
3. 'measurement of the earth'
4. The enciant Egypticians and the babylonians.
5. The Egypticians
6. The Babylonians
7. The Greeks
8. Thales and Pythagoras
9. Euclid
10. Elements
11. Brahamgupt, Bhaskar II, Aryabhatt
12. Axioms are the common nations (as sumptions) used throughout mathematics and not specially linket to gerometry.
Postupates are the assumptions specific to geometry.
13. A strainght line may be drawn from any Egypticians one point to any other point
14. A circle can be drawn with any radius and any centre.
15. All right angles are equal to one another.
16. If a staright line falling on two straight lines make the interior angles on the same side of it taken together less then two right angles, if produced indefinitely, meet on that side on which the sum of angles is less than two right angles.
17. John Playfair in 1729.
18. Playfair's Axiom
19. Two distinct intersecting lines cannot be parallel to the same line.
20. Axioms are the basic facts which are taken for granted without proof. They are obvious universal truth.

Theorems are statement which are proved through logical reasoning based on previously proved results and some Axioms.
21. Inspite of several attempts till today, this postulate could not be proved as a theo rem. Moreover, these attempts have led to the creation of different other geometries
known as non-euclidean geometries.
22. Two
23. One
24. Two distinct intersecting lines cannot be parallel to the same line.
25. Elements
27. No, Playfair's Axiom
29. XY, YZ, ZX
31. Equal
33. Same thing
35. Three, two half planes, line
37. perpendicular, perpendicular
39. Yes (Breadthless)
41. (i) $\mathrm{AC}, \mathrm{BQ}, \mathrm{RS}$
(ii) C,D, Q, S
(iii) $A C, B Q$
42. When two lines have a common point they are called intersecting lines.

When more then two lines have a common point, they are called concurrent lines.
43. If $I$ is a line and $P$ is point not on line $I$, there is one and only one line which passes, thnrough $p$ and is parallel to $I$.

44. Collinear
45. A point $C$ is said to lie between two points $A \& B$ if $A, B$ and $C$ are collinear points and $A C+C B=A B$
46. A point $M$ is said to be the mid point of $A B$ if $M$ is an interior point of $A B$ and $A M=M B$
47. If two line segments have equal lengths, they are congruent to one another.
48. A point is that which has no part.
49. A line is breadthless length.
50.
(i) True
(ii) False
(iii) True
(iv) True

## CHAPTER-6 <br> Lines and Angles

If a ray stands on a line, then the sum of the two adjacent angles so formed is $180^{\circ}$ and vice versa. This property is called as the Linear pair axiom.

In fig. 1

$$
\begin{gathered}
x \quad 90 \quad \frac{1}{2} y \\
\text { or } B O C \quad 90
\end{gathered} \begin{array}{lll} 
& \frac{1}{2} & B A C
\end{array}
$$



In fig. 2

$$
\begin{aligned}
& B O C \quad 90-\frac{1}{2} x \\
& \text { or } B O C \quad 90-\frac{1}{2} \quad B A C
\end{aligned}
$$



- If two lines intersect each other, then the vertically opposite angles are equal.
- If a transversal intersects two parallel lines :-
(i) Each pair of corrosponding angles are equal.
(ii) Each pair of alternate interior angles is equal.
(iii) Each pair of interior angles on the same side of the transversal
 is supplementary.

If a transversal intersects two or more lines :-
(a) Corrosponding angles
(i) 15
(ii) 26
(iii) 48
(iv) $3 \quad 7$
(b) Alternate exterior angles
(i) $1 \quad 7$
(ii) 28
(c) Alternate interior angles
(i) 46
(ii) 3
(d) Interior angles on the same side of a transversal
(i) $\quad 4 \quad 5 \quad 180$
(ii) $\quad 3 \quad 6 \quad 180$

- Lines which are parallel to a given line are parallel to each other.
- The sum of the three angles of a triangle is $180^{\circ}$.


| 4 | 1 | 2 |
| :--- | :--- | :--- |

Exterior angle property

## CHAPTER-6

## Lines and Angles

1. Name two pair of adjacent angles given in the adjoining figure.

2. In the figure find $\angle A O C$ if $\angle A O B=68^{\circ}$ and $\angle B O C=42^{\circ}$.

3. If $\angle X O Y$ and $\angle Y O Z$ are two adjacent angles, find the measure of $\angle X O Z$ if $\angle X O Y=56^{\circ}$ and $\angle Y O Z=34^{\circ}$.

4. If the angle is equivalent to its complement what is the measure of that angle?
5. What is the measure of the angle if its supplementary angle measure $98^{\circ}$.
6. Angles of a linear pair are in the ratio $8: 1$. What is the degree measure of both angles.
7. Find the value of $x$ from the adjoining figure.

8. If three angles $x, y$ andz are angles as shown in the figure. Find the value of $\frac{1}{2} z$ if $x=58^{\circ}$ and $y=42^{\circ}$

9. In the fig., find the value of $x+y$

10. In the fig. if OP is the bisector of $\angle A O C$ and OQ is the bisector of $\angle B O C$ then find $\angle P O Q$.

11. In fig. $\angle P E B=50^{\circ}$ and $A B \| C D$, then find $x$.

12. In fig. $\mathrm{p} \| \mathrm{q}, \angle 1=70^{\circ}$ then find $\angle 2$.

13. In fig. $\mathrm{p}\|\mathrm{q} \& \mathrm{r}\| \mathrm{s} \angle 1=80^{\circ}$ then find $\angle 3$.

14. In fig. $A B \| C D$ and $C D|\mid E F$, if $\angle A B C=30^{\circ}, \angle B C E=10^{\circ}$ then find $\angle C E F$.

15. In fig. $\mathrm{AB} \| \mathrm{CD}, \angle A B O=60^{\circ}, \angle A O B=20^{\circ}$ then find $\angle O D C$.

16. In fig. $\angle C B D=103^{\circ} \& \angle B A C=35^{\circ}$ find x and y .

17. In fig. $\angle P Q R=69^{\circ}, \angle Q P R=25^{\circ}$ find $\angle P R S$.

18. The angles of the triangle are in the ratio $2: 3: 4$. Find the angles of the triangle.
19. The angles of the triangle are in the ratio $1: 3: 6$. Find the angles of the triangle.
20. In fig. $l \| m \angle 1: \angle 2=3: 2$ find $\angle 3$.

21. In fig. OB and OC are bisectors of $\angle B$ and $\angle C$ of $\triangle A B C$ respectively. If $\angle B A C=62^{\circ}$ , $\angle A B C=54^{\circ}$, then find $\angle B O C$

22. in fig., if $\mathrm{AB} \| \mathrm{CD}, \angle \mathrm{APQ}=50^{\circ}$ and $\angle P R D=125^{\circ}$, find x and y .

23. lin fig., $\mathrm{PQ}||\mathrm{RS}|| \mathrm{AB} \angle M X Q=135^{\circ}$ and $\angle M Y R=40^{\circ}$, find $\angle X M Y$.

24. In fig. $A B \| C D$. Then find $x$.

25. In fig. $\angle S P R=135^{\circ}$ and $\angle P Q T=110^{\circ}$ then find $\angle P R Q$.

26. The complementary angle of any given angle is $2^{0}$ more than the thrice of that angle. What is the measure of angles.
27. The angle and its supplementary angle are in the ratio $2: 3$. What is the measure of each angle.
28. In fig. $A B$ and $C D$ are straight lines which intersects at the point $O$. If $\angle 1=70^{\circ}$ and $O E$ bisects $\angle B O D$ then find $\angle 2$.

29. If complementary angle of an angle is twice the angle. Then find the angle.
30. If complementary angle of an angle is $2^{0}$ more than the angle. Then find the angle.
31. In fig. $\angle B O P=40^{\circ}, O Q$ bisects $\angle A O P$. Find $\angle A O Q$.

32. In fig. $\angle A C D$ is twice of $\angle A C B$, if $\angle B A C=50^{\circ}$, then find $\angle A B C$.
33. If I\|m amd $m \| n$ then find $x$.

34. I||m, if $\angle 1: \angle 2=7: 3$ then find $\angle 1$ and $\angle 2$.

35. In fig. I\|m, if $\angle 1: \angle 2=2: 3$ then find $\angle 3$.

36. In fig. $\angle B A C=80^{\circ}$ and $\angle A B C=40^{\circ} B O$ and $C O$ are the bisectors of $\angle A B C$ and $\angle A C B$ respectively. Then find $\angle B O C$.

37. If $C E$ is the bisector of $\angle A C D$ and $C E \| B A$ and $\angle A C D=130^{\circ}$. Then find $\angle B A C$.

38. If RT is the bisector of $\angle P R S$ and $\mathrm{PQ} \| \mathrm{RT}$ and $\angle P R S=110^{\circ}$. Then find $\angle P Q R$.

39. In fig. BO and CO are bisectors of external angle at B and C respectively. If $\angle B A C=80^{\circ}$ and $\angle A B C=40^{\circ}$. Then find $\angle B O C$.

40. In fig. I||m. If $\angle 1=45^{\circ}$, then find $\angle 2$.

41. In fig. I\|m, AM and BN are prependicular to I and m respectively. If AM bisects $\angle P A B$ and BN bisects $\angle A B Q$ and $\angle 1=30^{\circ}$, then find $\angle 2$.

42. Find the value of $x$.

43. Find the value of $x$.

44. In the fig. find the value of $x$.

45. In fig. if $\angle P=100^{\circ}$ and $\angle R=40^{\circ}$, then find $\angle P Q S$.

46. In fig. if $\angle B A C=50^{\circ}, \angle A B E=90^{\circ}$, then find the value of $y$.
47. In fig. I\|m, then find the value of $x$.

48. In fig. $1 \| \mathrm{m}$ and $\mathrm{p} \| \mathrm{q}, \angle 1=100^{\circ}$, Then find value of $\angle 2$

49. In the fig. $\mathrm{PS}\|\mathrm{QR}\| \mathrm{TA}, P T \perp T A, \angle Q T R=30^{\circ}$, find the value of $\mathrm{x}, \mathrm{y}, \mathrm{z}$.

50. In the fig. $B M \perp A C, \angle M B C=35^{\circ}, \angle P A C=40^{\circ}$, find the value of x .


## CHAPTER 6 <br> Answer <br> ( Lines and Angles )

1. $\angle A B C$ and $\angle D B C ; \angle B E F$ and $\angle A E F \quad \angle A O C=26^{\circ}$
2. $\angle X O Z=90^{\circ}$
3. Each angles is equal to $45^{\circ}$
4. $82^{0}$
5. $160^{\circ}$ and $20^{\circ}$
6. $x=10^{\circ}$
7. $\frac{1}{2} z=40^{0}$
8. $x+y=260^{\circ}$
9. $\angle P O Q=90^{\circ}$
10. $x=130^{\circ}$
11. $\angle 2=70^{\circ}$
12. $\angle 3=100^{\circ}$
13. $\angle C E F=160^{\circ}$
14. $\angle O D C=100^{\circ}$
15. $x=68^{\circ}, y=77^{\circ}$
16. $\angle P R S=94^{0}$
17. $40^{0}, 60^{\circ}, 80^{0}$
18. $18^{0}, 54^{0}, 108^{0}$
19. $\angle 3=72^{0}$
20. $\angle B O C=121^{\circ}$
21. $x=50^{\circ}, y=75^{\circ}$
23.. $\angle X M Y=85^{\circ}$
22. $x=130^{\circ}$
23. $\angle P R Q=65^{\circ}$
24. $22^{0}, 68$
25. $72^{0}, 108^{0}$
26. $\angle 2=55^{\circ}$
27. $30^{0}$
28. $\angle A B C=70^{\circ}$
29. $\angle 3=108^{0}$
30. $\angle P Q R=55^{\circ}$
31. $\angle 2=30^{\circ}$
32. $x \quad 30^{0}$
33. $x=70^{\circ}$
34. $95^{0}$
35. $44^{0}$
36. $\angle A O Q=70^{\circ}$
37. $\angle 1=126^{\circ}, \angle 2=54^{0}$
38. $\angle B A C=65^{\circ}$
39. $\angle 2=45^{\circ}$
40. $x=65^{0}$
41. $y=40^{0}$
42. $\angle x=120^{\circ}, \angle y=120^{\circ}, \angle z=60^{\circ}$

## (Chapter-7)

## Triangles

- Two figures are congurent, if they are of the same shape and the same size.
- If two triangles ABC and PQR are congruent under the correspondence $A \quad R, B \quad C$ and $C \quad R$, then symbolically it is expressed as $A B C \quad P Q R$
- Two circles of the same radii are congruent.

If two sides and the included angle of one triangle are equal to two sides and the included angle of the other triangle, then the two triangles are congruent (SAS congruence rule)

- If two angles and the included side of one triangle are equal to two angles and the included sides of the other triangle, then the two triangles are congruent by (ASA Congruence Rule)

If two angles and one side of one triangle are equal to two angles and the corresponding side of the other triangle, then the two triangles are congruent by (AAS Congruence Rule)

Angle opposite to equal sides of a triangle are equal.

Sides opposite to equal angles of a triangle are equal.

Each angle of equilateral triangle is $60^{\circ}$.

If all the sides of one triangle equals to all sides of the other triangle, then the triangles are congruent (SSS Congruence Rule)

If the two right triangles, hypotenuse and one side of one triangle are equal to the hypot enuse and one side of the other triangle, then the two triangles are congruent (RHS Congruence Rule)

- In a triangle, angle opposite to the longer side is larger.
- In a triangle, size opposite to the larger (greater) angle is longer.
- Sum of any two sides of a triangle is greater than the third side.


## (Chapter-7)

## Triangles

1. Two triangles given in the figure are congruent. Give the correspondence between the triangles?

2. Which criterion (or congruence rule) is used for the congruency of two triangles?

3. In the figure which two triangles are congruent?
4. In the figure which congruency rule is used to prove that SQ bisects PR.

5. In the figure $\mathrm{PQ}=\mathrm{PR}=\mathrm{PS}$. Find $\angle Q R S$
6. In the figure find $x$ if $B C=A D$ and $A B=C D$.

7. In the figure $P Q \| S R$ and $P S=Q R$. Find $2 x$

8. In the figure

$$
\begin{array}{cccc}
L M & M N, & Q M & M R \\
L M & P Q, & M N & P R
\end{array}
$$

$$
\angle Q=50^{\circ} . \text { Find } \quad x
$$


9. In the figure $\mathrm{AB}=\mathrm{BC}$, and $\angle A=\angle C$. Find $x$.
10.
 In $\triangle A B C, A B=A C$ and $\angle 1=\angle 2, A \quad 40^{\circ}$. Find $\angle P B C$ and $\angle P C B$.
11. In the figure ABC is an equilateral triangle. Find $x \quad y$.

12. In a right angled triangle one acute angle is double the other. Find both the angles.
13. In a triangle, sum of two sides of a triangle is always $\qquad$ than the third side.
14. In a figure find $x \quad y$.

15. In the figure $A B C D$ is a square. Sides $A B$ and $B C$ are produced to points $P$ and $Q$ such that $B P=C Q$. If $D P=7 \mathrm{cms}$. Find $A Q$.
16. In the figure find $x$.

18. In the figure $A B C$ and PBC are two isosceles triangles. Find $x$.

19. $X Y Z$ and $P Y Z$ are two isosceles triangles on the same base $Y Z$. If $\angle P=120^{\circ}$ and $X Y P \quad 40^{\circ}$. Find $x$.
20. In a triangle angle opposite to longer side is $\qquad$

21. In the figure which is the longest side?

22. Which angle of $X Y Z$ is greatest?

23. In quadrilateral $A B C D, A B=A D$ and $B C=C D$. Find $x$.

24. Angles opposite to equal sides of a triangle are $\qquad$ .
25. In a right angled triangle hypotenuse is the $\qquad$ side.
26. In the figure find $x$.

27. In the given figure $X Y Z$ is a right angled triangle. If $X Y=8 \mathrm{~cm}$ and $Y Z=4 \mathrm{~cm}$. Find $X Z$.

28. In the figure $\angle A=\angle D=30^{\circ}$. Find $x+y$.

30. In a triangle $A B C$, sides $A B=5 \mathrm{cms}$. $B C=3 \mathrm{cms}$ and $A C=5.5 \mathrm{cms}$. Which angle is the largest angle?
31. From the given figure find $x$.

32. In the figure $\angle P=24^{\circ}, \angle Q=46^{\circ}$ and $\angle S=40^{\circ}$. Find $x$.

33. In the figure $A C$ bisects angles $\angle A$ and $\angle C$. If $A B=3 \mathrm{~cm}$. Find $A D$.

34. In the figure $l \| m, A C=D B$. Find $C D$ and $A B$.

35. Find $P Q$ from the figure. If $P A=Q B$.
36. Find $\angle B A C$ if $A C=B C$.

37. In the figure $D E \| B C$. Find $x \quad y$.
38.
n the adjoining figure $D B C \quad E A F$. If $\mathrm{AB}=4 \mathrm{~cm}$. Find $\mathrm{FC}=$ ?

39. In $A B C, A B=A C . \angle D B C=\angle D C B=40^{\circ}$. Find x .

40. In a triangle sum of three altitudes is $\qquad$ than the perimeter of the triangle.
41. In a triangle perimeter is $\qquad$ than the sum of three medians.
42. In the figure $P Q R$ is an isosceles triangle, $\mathrm{PQ}=\mathrm{PR}$. If $\angle 1>\angle 2$, what is the relation between $x$ and $y$.

43. In the figure $\triangle A B C$ and $\triangle D E F$ are equilateral triangles. Give the measure of $\angle A, \angle D, \angle F$.

44. In the figure $\mathrm{BA}=\mathrm{BD}$. If $\angle A B D=48^{\circ}$ find $x$.

45. From the figure find $x$.


## Triangles (Chapter-7) <br> Answers

1. $A B=X Y=3 \mathrm{~cm}$
$B C=X Z=5 \mathrm{~cm}$
$C A=Z Y=4 c m$
2. Side-Angle-Side (SAS) Criterion
3. BOC AOD
4. AAS criterion or ASA criterion
5. $\angle Q R S=90^{\circ}$
6. $\quad x \quad 75^{\circ}$
7. $\quad 2 x$ y $180^{\circ}$
8. $\times 40^{\circ}$
9. $x \quad 50$
10. $\angle P B C=15^{\circ}$
$\angle P C B=15^{\circ}$
11. $\quad A Q=7 \mathrm{~cm}$
12. $\times 50^{\circ}$
13. $\times 55^{\circ}$
14. $x \quad 115^{\circ}$
15. $\times 40^{\circ}$
16. Greater
17. BC
18. $X$
19. $\times 105^{\circ}$
20. Equal
21. Longest
22. $x=80^{\circ}$
23. $X Z=4 \sqrt{5} \mathrm{~cm}$
24. $x$ y $120^{\circ}$
25. $360^{\circ}$
26. $A B 6 \mathrm{~cm}$

CD 8 cm
35. $P Q=8 \mathrm{~cm}$
36. $\angle A=57.5^{\circ}$
37. $x$ y $140^{\circ}$
38. $\mathrm{FC}=4 \mathrm{~cm}$
39. $x=130^{\circ}$
40. Less
41. Less
42. $y x$
43. $\angle A=60^{\circ}, \angle D=60^{\circ}$,
$\angle F=60^{\circ}$
44. $x=114^{\circ}$
45. $x=45^{\circ}$
11. $240^{\circ}$
12. $30^{\circ}, 60^{\circ}$
13. Greater
14. $x$ y $120^{\circ}$
30. $\angle B$
31. $x 135^{\circ}$
32. $x \quad 110^{\circ}$
33. $A D=3 \mathrm{~cm}$

## (Chapter-8)

## QUADRILATERALS

- A quadrilateral has four sides, four angles and four vertices.
- The sum of angles of a quadrilateral is $360^{\circ}$.
- In a parallelogram (IIgm) :-
(i) Opposite sides are equal.
(ii) Opposite angles are equal.

(iii) Diagonal bisects each other

A quadrilateral is a parallelogram if :-
(i) Opposite sides are equal.
(ii) Opposite angles are equal.
(iii) Diagonals bisect each other.
(iv) A pair of opposite sides is equal and parallel.

- Note that a square, rectangles and rhombus are all parallelogram.
- A square is a rectangle and also a rhombus.
- A parallelogram is a trapezium.
- A kite is not a parallelogram.
- A trapezium is not a parallelogram.
- A rectangle or a rhombus is not a square.


Square


Rectangle


Rhombus

Diagonals of a rectangle bisects each other and are equal.

Diagonals of a rhombus bisect each other at right angles.

Diagonals of a square bisects each other at right angles.

- The line segment joining the mid points of any two sides of a triangle is parallel to the third side and is half of it. And this is the mid point theorem.
- The quadrilateral formed by joining the mid points of the sides of a quadrilateral, in order is a parallelogram.
- $\quad A B C D$ is a quadrilateral.
- $\quad P, Q, R$ and $S$ are mid points of the sides $A D, A B, B C$ and $C D$.
- PQRS is a llgm.


If all the four vertices of the quadrilateral lie on a circle then the quadrilateral is called cyclic quadrilateral.

Sum of opposite angles of a cyclic quadrilateral is $180^{\circ}$.


A $\quad$ C 180
B $\quad D 180$

If the sum of pair of opposite angles of a quadrilateral is $180^{\circ}$, the quadrilateral is cyclic.

## AREA OF PARALLELOGRAMS \& TRIANGLES

- Two congruent figures have equal areas but the converse need not to be true.

Parallelograms on the same base (or equal bases) and between the same parallels are equal in area.
$\operatorname{ar}(\mathrm{ABCD})=\operatorname{ar}(E F C D)$

- Area of IIgm = Base $\times$ Altitude


Ilgm of the same base and having equal areas lie between the same parallels.

If the parallelogram and the triangles are on the same base and between the same parallels, then area of the triangle is half the area of the parallelogram.
$\operatorname{ar}(E D C) \frac{1}{2} \operatorname{ar}(A B C D)$


- Triangles on the same base and between the same parallels are equal in area.
- Area of a triangle $=\frac{1}{2} x$ base $x$ altitude
$\checkmark \quad$ Triangles on the same base and having equal areas lie between the same parallels.

A median of a triangle divides it into two triangles of equal areas. $\operatorname{ar}(x) \operatorname{ar}(y)$. If AD is median.


## (Chapter-8)

## Quadrilaterals

1. What is the sum of all interior angles of a quadrilateral?
2. If four angles of a quadrilateral are in the ratio of $1: 2: 4: 5$. Find the angles.
3. In a quadrilateral, if two $\angle \mathrm{s}$ are right angles and other two angles are in the ratio 1:2. Find these angles.
4. In a quadrilateral, if two $\angle s$ are complementary and other two $\angle s$ are in the ratio 4:5. Find the measure of these two $\angle s$.
5. Three $\angle s$ of a quadrilateral, are $49^{\circ}, 70^{\circ}$ and $121^{\circ}$. Find the fourth angle.
6. In the given figure find the value of $x$.

7. If four angles of a quadrilateral are in the ratio $2: 3: 6: 7$. Find the four angles.
8. In a || gm if, one angle is $90^{\circ}$ then find the other three angles.
9. In the given figure $A B C D$ is $\| g m$. Find $\angle D$
10. In the figure PQRS is $\| g m$. Find $\angle x$.

11. In the given figure $A B C D$ is a $\| g m$.

Find $\angle D$ and $\angle C$.

12. In given ABCD is a $\| \mathrm{gm}$. Find $\angle A D C$.

13. Find $x+y$ in the given figure if PQRS is a \|lgm.

14. In the given figure $P Q R S$ is a rectangle. Find $P R+Q S$.

15. Find $x y$ in the $\| g m$ MNOP.

16. $A B C D$ is a rhombus. Find the perimeter of $A B C D$.

17. Find the sum of length of diagonals in Rhombus PQRS.

18. Four angles of a quadrilateral are in the ratio $3: 5: 9: 13$. Find the measure of greatest angle.
19. In a quadrilateral, if one angle is of measure $100^{\circ}$ and other three angles are in the ratio 1:5:7 then find the measure of other three $\angle s$.
20. In the figure find $\angle A \& \angle C$ if $A D=D C$ and $A B=B C$

21. In a Rhombus $A B C D$ find the sum of $\angle B+\angle C$.
22. In the given figure $A B C D$ is a rectangle in which $B A C \quad 57^{\circ}$. Find $\angle D B C$.

23. Perimeter of given \|gm is 128 m . Find the value of x .

24. Find the value of $\angle B+\angle D$ in the given $\| g m$ ABCD.

25. Find the value of $x$ and $y$ in the given figure, if $A B C D$ is a $\| g m$.

26. If the perimeter of a || gm is 14.6 cm and the longer side is 4.8 cm . Find the length of shorter side.
27. If the ratio of the base and area of a $\| g m$ is $1: 8$ then find the length of its altitude.
28. If the ratio of the altitude and the area of the $\| g m$ is $2: 11$. Find the length of the base of $\| \mathrm{gm}$.
29. Find the area of $A B C$ in the given $\| g m$ ABCD.

30. Find the area of $\| \mathrm{gm} A B C D$ if $A P=5 \mathrm{~cm}$ and $B D=22 \mathrm{~cm}$.

31. In the given figure find the perimeter of || gm ABCD.

32. In the given figure PQRS is a $\| \mathrm{gm}$ in which $\mathrm{PQ}=12 \mathrm{~cm}, \mathrm{ST}=9 \mathrm{~cm}, \mathrm{QM}=6 \mathrm{~cm}$. Find the length of SP.

33. Find the area of $A E B$ if area of $\| g m$ ABCD is 184 sq.cm.

34. Find the ratio of the area of $P T Q$ and rectangle PQRS.

35. In the given figure $P Q\|S R, N R\| P Q$ and $N P \| M Q$ find the area of $P Q R N$ if $P Q=9 \mathrm{~cm}$, $\mathrm{ST}=5 \mathrm{~cm} \& \mathrm{SM}=3 \mathrm{~cm}$.

36. In the given figure $A D\|B C, E C\| A B$ and $E$ is mid point of $A D$. If area of $A B C D$ is 96 sq.cm. find the area of $\triangle E D C$.

37. In the given figure $D, E, F$ are the mid points of sides $A B, B C$ and $A C$ respectively. If $\angle A=50^{\circ}, \angle B=60^{\circ}$ and $\angle C=70^{\circ}$. Find $\angle D, \angle E$ and $\angle F$

38. Area of rectangle $A B C D$ and $\| g m$ ABEF are equal in area. If base $A B=8 \mathrm{~cm}$ and height of $B C=3 \mathrm{~cm}$. Find the perimeter of $\| g m A B E F$ if $C$ is the mid point of $E F$.
39. In the given $\triangle A B C, D$ and $E$ are the mid point of $A B$ and $A C$. Find the length of $D E$ and measure of $\angle A$

40. $\quad A D$ is the median of $\triangle A B C$. If area of $\triangle A B D=x \mathrm{~cm}^{2}$ and area of $\triangle A B C$ is $y \mathrm{~cm}^{2}$. What is the relation between $x$ and $y$ ?

## Quadrilaterals (Chapter-8) Answers

| 1. | $360^{\circ}$ | 19. | $20^{\circ}, 100^{\circ}, 140^{\circ}$ | 37. | $70^{\circ}, 50^{\circ}, 60^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2. | $30^{\circ}, 60^{\circ}, 120^{\circ}, 150^{\circ}$ | 20. | $130^{\circ}, 130^{\circ}$ | 38. | 26 cm |
| 3. | $60^{\circ}, 120^{\circ}$ | 21. | $180^{\circ}$ | 39. | $6 \mathrm{~cm}, 60^{\circ}$ |
| 4. | $120^{\circ}, 150^{\circ}$ | 22. | $33^{\circ}$ | 40. | $y=2 x$ |
| 5. | $120^{\circ}$ | 23. | 8 |  |  |
| 6. | $x=20^{\circ}$ | 24. | $200^{\circ}$ |  |  |
| 7. | $40^{\circ}, 60^{\circ}, 120^{\circ}, 140^{\circ}$ | 25. | $x=6, y=5$ |  |  |
| 8. | $90^{\circ}, 90^{\circ}, 90^{\circ}$ | 26. | 2.5 |  |  |
|  |  | 27. | 8 Unit |  |  |
| 9. | $130^{\circ}$ |  |  |  |  |
|  |  | 28. | 5.5 Unit |  |  |
| 10. | $50^{\circ}$ |  |  |  |  |
|  |  | 29. | 38sq.cm |  |  |
| 11. | $60^{\circ}, 120^{\circ}$ |  |  |  |  |
|  |  | 30. | 110sq.cm |  |  |
| 12. | $110^{\circ}$ | 31. | 32 cm |  |  |
| 13. | $64^{\circ}$ | 32. | 18 cm |  |  |
| 14. | 26 cm | 33. | 92sq.cm |  |  |
| 15. | $105^{\circ}$ | 34. | 1:2 |  |  |
| 16. | 20 cm | 35. | 60sq.cm |  |  |
| 17. | 62 cm | 36. | 32sq.cm |  |  |
| 18. | $156^{\circ}$ |  |  |  |  |

## (Chapter-9)

## Circles

- A circle divides the plane on which it lies into three parts.
(i) Interior
(ii) The circle
(iii) Exterior

$-\quad$ The longest chord of a circle is a diametre of a circle.

Major segment or Major sectors


Equal chords of a circle subtend equal angles at the centre.

If the angle subtended by two equal chords of a circle at the centre are equal, the chords are equal.

- The perpendicular from the centre of a circle to a chord bisects the chord.
- The line drawn through the centre of a circle to bisect a chord is prependicular to the chord.
$\bullet \quad$ There is one and only one circle passing through three non collinear points.

Equal chords of a circle are equidistant from the centre.

- Chords equidistant from the centre of a circle are equal.
- Congruent arcs of a circle subtend equal angles at the centre.
- The angle subtended by an arc at the centre is double the angle subtended by it at any point on the remaining part of the circle.
- Angle in the same segment of a circle are equal.

Angle in a semi circle is a right angle.

## (Chapter-9)

## Circles

1. How many circles can be drawn through three non-collinear points?
2. In the given figure, D is the mid point of chord AB . Find $\angle O D A$.

3. $A B C D$ is a cyclic quadrilateral. If $A 95^{\circ}$ then find the measure of $\angle C$.
4. In the figure $A O B 120^{\circ}$. Find $A C B$.

5. In the figure chord $A B$ is at a distance of 4 cm from the centre $O$ of the circle. If the radius of circle is 5 cm . Find the length of chord $A B$.
6. In a circle with center $O, \angle A O B=60^{\circ}$. Find reflex $\angle A O B$.

7. If ABCD is a cyclic quadrilateral, what is the sum of $\angle A$ and $\angle C$ ?
8. What type of angle is formed in a Major segment of a circle?
9. What is the type of angle formed in a Minor segment of a circle?
10. If AB is a diameter of a circle with center $\mathrm{O} . \mathrm{C}$ is any point on the circle. Find $\angle A C B$.
11. In the figure $A B C D$ is a cyclic quadrilateral. Side $D C$ of the quadrilateral is produced to point $P$. If $\angle B C P=110^{\circ}$, find $\angle A$.

12. In the figure $A B C D$ is a cyclic quadrilateral. Side $C D$ is produced to both sides so that $\angle B C P=110^{\circ}$ and $\angle A D Q=95^{\circ}$. What is the sum of angles $\angle A$ and $\angle B$ ?

13. ABCD is a cyclic quadrilateral. If $\angle A=110^{\circ}$ and $\angle B=60^{\circ}$. Find the sum of $\angle B$ and $\angle C$.
14. In the adjoining figure, chord $A B$ is at a distance of 5 cms from centre $O$ of the circle. Find radius of circle if length of the chord is 24 cm .

15. In the figure length of the chord of a circle of radius 25 cms is 48 cm . Find the distance of chord from the centre of circle.

16. In a circle with centre $O$, two chords $A B$ and $C D$ are equidistant from the centre. If $A B=8$ cm , what is the length of CD ?
17. In the figure $\angle A O B=140^{\circ}$. Find $\angle A D B$.
18. In the figure, find $\angle B O C$.

19. ABCD is a cyclic quadrilateral in which $A B \| C D$. If side $C D$ is produced to both sides and $\angle A D Q=80^{\circ}$ then find $\angle B C P$.

20. The two angles $\angle P$ and $\angle R$ of a cyclic quadrilateral $P Q R S$ are in the ratio 1:2. Find the two angles $\angle P$ and $\angle R$.
21. In the figure $A B C D$ is a cyclic quadrilateral in which $A B \| C D$ and $A D \| B C$. Find $\angle D A B$.
22. In the figure $\angle A B C=75^{\circ}$. Find $\angle A D C$.

23. In the figure $A B C E$ is a cyclic quadrilateral. If $\angle A E C=80^{\circ}$, then find $\angle A D C$.
24. In the figure find $x$.

25. Greatest chord of a circle is called $\qquad$ .
26. Complete the sentence :- In a circle the chord nearer to the centre of circle is $\qquad$ .
27. A chord of a circle subtend equal angles at two points on the same side of the chord, then the four points are $\qquad$ .
28. Find $x$ in the figure.

29. Find $x$ in the figure.

30. In the figure $P Q=R S$ and $P S$ is the diameter of the circle. Find $x$.

31. In the figure diagonal of a cyclic quadrilateral passes through the centre $O$ of the circle. Find the measures of $\angle B$ and $\angle D$.

32. Diagonals of a cyclic quadrilateral $A B C D$ passes through the centre of the circle. What type of quadrilateral is $A B C D$ ?
33. Two diameters of a circle are perpendicular to one another. What is the type of quadrilateral formed by joining the four points?
34. In the figure $A B C D$ is a cyclic quadrilateral in which $A B \| C D$ and $\angle D=80^{\circ}$. Find $\angle C$.

35. In the circle $\mathrm{C}(\mathrm{o}, \mathrm{r}), \overparen{A B}=\overparen{C D}$. Find the length of chord $A B$.
36. In the figure chord $\mathrm{AB}=$ chord BC . If $\angle A O B=60^{\circ}$ then find $\angle A O C$.

37. In the figure $A B$ is the chord of circle which centre $O$. Chord $A B$ is produced to point $C$ in such a way that $\mathrm{BC}=\mathrm{OB}$. If $\angle O C B=30^{\circ}$ then find $\angle A O B$.

38. In the figure, two chords $A B$ and $A C$ of a circle are equal. AM is the bisect of $\angle C A B$. Find where is centre of circle?
39. In figure $O D \perp A B$. If $O D=3 \mathrm{~cm}$, find $A C$.

40. In the figure $O D \perp B C$. If $O$ is the circumcenter of $A B C$ then find $\angle O B D$.
41. In the figure find $x$.

42. In the figure $A B C D E$ is a pentagen in the semicircle.

Find $\angle A B C+\angle C D E$.
43. In the figure $A C=B D$. Find the relation between $\angle A$ and $\angle B$ also find $\angle B$.
44. In the figure find $\angle R T Q$ and $\angle R Q T$.

45. In the figure two concentric circles with centre $O$ have a common tangent AD cutting the inner circle at B and C .
If $O M \perp A D, A D=18 \mathrm{~cm}$ and $B M=8 \mathrm{~cm}$. Find $A B$.

46. $A B$ and $A C$ are two equal chords of a circle $O D \perp A B$ and $O E \perp A C$. What type of triangle is $A D E$ ?

47. Two circles with centres O and $O^{1}$ intersect at A and B . Find $\angle P B Q$.

48. PQ is a chord of circle with radius ' r '. If A is any point on the circle such that $\angle P A Q=90^{\circ}$ then find $P Q$.
49. In the figure, $O$ is the centre of circle with radius 5 cm . If $O P \perp A B, O Q \perp C D$ and $A B \| C D$, $A B=8 \mathrm{~cm}, C D=6 \mathrm{~cm}$. Find $P Q$.


## Circles (Chapter-9) <br> Answers

1. One
2. $90^{\circ}$
3. $85^{\circ}$
4. $60^{\circ}$
5. 6 cm
6. $300^{\circ}$
7. $180^{\circ}$
8. Acute angle
9. Obtuse angle
10. $90^{\circ}$
11. $110^{\circ}$
12. $205^{\circ}$
13. $130^{\circ}$
14. 13 cm
15. 7 cm
16. 8 cm
17. $110^{\circ}$
18. $160^{\circ}$
19. $80^{\circ}$
20. $\angle P=60^{\circ}$ and $\angle R=120^{\circ}$
21. $90^{\circ}$
22. $75^{\circ}$
23. $100^{\circ}$
24. $48^{\circ}$
25. Diameter
26. Greater
27. On the circle
28. $30^{\circ}$
29. $30^{\circ}$
30. $75^{\circ}$
31. B $90^{\circ}$ and

D $90^{\circ}$
32. Rectangle
33. Square
34. $80^{\circ}$
35. Equal to chord CD
36. $120^{\circ}$
37. $60^{\circ}$
38. On the line $A M$
39. 6 cm
40. $26^{\circ}$
41. $65^{\circ}$
42. $270^{\circ}$
43. $\angle A=\angle B$ and $\angle B=48^{\circ}$
44. $\angle R T Q=45^{\circ}$ and $\angle R Q T=110^{\circ}$
45. 1 c.
46. Isosceles triangle
47. $180^{\circ}$
48. 2 r
49. 7 cm

## (Chapter-10)

## Heron's Formula

- Area of a triangle with its sides as a, b and c - by using Heron's formula

Area of Triangle $=\sqrt{s(s-a)(s-b)(s-c)}$
where $s \frac{a b c}{2}$

Area of quadrilateral whose sides and one diagonal are given, can be calculated by dividing the quadrilateral into two triangles and using the Heron's formula.

- To multiply any number by -11
-> let take no. 132
$132 \times 11=$ $\qquad$
$\rightarrow \quad 132 \times 11=1(3+1)(3+2) 2$
$132 \times 11=1452$
- Area of equilateral triangle $=\frac{\sqrt{3}}{4} x(s i d e)^{2}$


## (Chapter-10)

## Heron's Formula

1. Give Heron's formula for finding area of triangle.
2. What are $a, b$ and $c$ used in Heron's formula?
3. If $a=12 \mathrm{~cm}, \mathrm{~b}=13 \mathrm{~cm}, \mathrm{c}=15 \mathrm{~cm}$, what is the value of s ?
4. In the triangle given below which sides are represented by $a, b$ and $c$ ?

5. Fill in the blank :- $s=\frac{?}{2}$
6. If $\mathrm{a}=25 \mathrm{~cm}, \mathrm{~b}=15 \mathrm{~cm}$ and $\mathrm{c}=20 \mathrm{~cm}$, what is the value of $(\mathrm{s}-\mathrm{b})$ ?
7. Sides of a triangular plot are in the ratio $2: 3: 4$ and its perimeter is 36 then the three sides are $\qquad$ and $\qquad$ _.
8. Find $s$ if

9. Area of an equilateral triangle with side 6 cm is $\qquad$ ?
10. In a triangle $\mathrm{a}=15 \mathrm{~cm}, \mathrm{~b}=7 \mathrm{~cm}$ and $\mathrm{s}=15 \mathrm{~cm}$, find the length of side C .
11. In an equilateral triangle $\mathrm{s}=30 \mathrm{~cm}$, what is the length of each side?
12. Area of triangle when Heron's formula is applied is $\sqrt{15 \times 9 \times 5 \times 3}$. Find it in simplified form.
13. Evaluate $\sqrt{18 \times 8 \times 9}=$ ?
14. If in a triangle $s-a=7 \mathrm{~cm}, \mathrm{~s}-\mathrm{b}=8 \mathrm{~cm}$ and $\mathrm{s}-\mathrm{c}=6 \mathrm{~cm}$, then $\mathrm{s}=$ ?
15. In an equilateral triangle with one side $x$ $s=$ ? $x$.
16. In a triangle ABC, $a=3 b=6 c$ then $S=$ ? $\times C$. Complete it.
17. In the adjoining figure, find s for $\triangle A B D$ and $\triangle B C D$.

18. The sides of a triangle are in the ratio $2: 3: 5$. If the perimeter of triangle is 50 m . Find the three sides.
19. The three sides of a triangle are $a=12 \mathrm{~cm}, \mathrm{~b}=14 \mathrm{~cm}, \mathrm{c}=20 \mathrm{~cm}$. Complete it :Area of triangle is $\sqrt{\_^{\times} \times 9 \times 3}$
20. If $\mathrm{s}-\mathrm{a}=12 \mathrm{~cm}, \mathrm{~s}-\mathrm{b}=9 \mathrm{~cm}, \mathrm{~s}-\mathrm{c}=4 \mathrm{~cm}$, then $\mathrm{s}=$ ?
21. In a triangle $A B C$, side opposite to vertex $B=\underline{?}$ and side opposite to vertex $C=\underline{?}$
22. Complete it :- Area of equilateral triangle $=\frac{\sqrt{3}}{4} \times$
23. In an equilateral triangle $s \quad \frac{3}{2} \quad a$. Find perimeter of the triangle.
(Where $a$ is the side of triangle)

## Heron's Formula (Chapter-10) <br> Answers

1. $\sqrt{s(s-a)(s-b)(s-c)}$
2. $a, b$ and $c$ are sides of the triangle
3. 20 c.m.
4. $A B \quad c, B C \quad a, A C \quad b$

Can take any of the sides as $\mathbf{a}$, 2nd $\mathbf{b}$ and remaining $\mathbf{c}$.
5. $a+b+c$
6. $\quad 15$ c.m.
7. $8 \mathrm{~cm} ., 12 \mathrm{~cm}$. and 16 cm .
8. $\quad 9 \mathrm{~cm}$.
9. $\quad 9 \sqrt{3} \mathrm{~cm}^{2}$
10. 8 cm .
11. 20 cm .
12. 45 unit $^{2}$
13. 36
14. 21 cm
15. $\frac{3}{2}$
16. $\frac{9}{2}$
17. 40 cm each
18. $10 \mathrm{~cm} ., 15 \mathrm{~cm} ., 25 \mathrm{~cm}$.
19. $\sqrt{23 \times 11 \times 9 \times 3}$
20. 25 cm .
21. $A C, A B$
22. $a^{2}$ or side ${ }^{2}$
23. 3 a
(Chapter-11)

## Surface Area And Volume

Useful 2-dimensional figures

| FIGURE | AREA | Perimeter / Circumferance |
| :---: | :---: | :---: |
| SQURE | A = Side $\times$ Side | $\mathrm{P}=4 \mathrm{x}$ side |
| RECTANGLE | A $=$ length $x$ breadth | $\mathrm{P}=2(\mathrm{l}+\mathrm{b})$ |
| TRIANGLE | A $=1 / 2 \times$ base $\times$ altitude | $\mathrm{P}=$ sum of three sides |
| Ilgm | A $=$ base $\times$ altitude | $\mathrm{P}=2 \times$ sum of adjecent sides |
| RHOMBUS | $A=b x h$ or $1 / 2 d_{1} \times d_{2}$ | $\mathrm{P}=4 \mathrm{x}$ sides |
| TRAPEZIUM | $A=1 / 2$ (sum of II sides) $\times \mathrm{h}$ | $P=$ sum of 4 sides |
| EQUILATERAL | $A=\frac{\sqrt{3}}{4} x(\text { side })^{2}$ | $\mathrm{P}=3 \mathrm{x}$ side |
| CIRCLE | A $=x$ (radius) ${ }^{2}$ | $\mathrm{C}=2 \mathrm{x}$ (radius) |
| SEMI CIRCLE | $A=1 / 2 \quad r^{2}$ | $C=r+2 r$ |

Cuboid
$\left(\begin{array}{lll}l & b & h\end{array}\right)^{2}(\text { Diagonal })^{2}$ 2(lb bh lh)


3 - Dimensional Figures

| Shape | Volume | Curved or lateral surface area | Total surface area |
| :---: | :---: | :---: | :---: |
| CUBOID | $V \quad l \quad b \quad h$ | $2(l) b$ | $S$ 2(lb bh lh) |
| CUBE | $V a^{3}$ | $4 a^{2}$ | $S 6 a^{2}$ |
| CYLINDER | $V \quad r^{2} h$ | $S 2 r h$ | $S 2 r(h r) 2 r h \quad r^{2}$ if open at the top |
| CONE | $V 1 / 3 r^{2} h$ | $\begin{aligned} & S \quad r l \text { where } \\ & l \\ & l \sqrt{h^{2} \quad r^{2}} \end{aligned}$ | $S r l r^{2}$ |


| SPHERE | $V$ | $4 / 3$ | $r^{3}$ | 4 | $r^{2}$ |  | $S$ | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| HEMISPHERE | $V$ | $2 / 3$ | $r^{3}$ | $S$ | 2 | $r^{2}$ |  |  |
| $S$ | 3 | $r^{2}$ |  |  |  |  |  |  |

Cube / Cuboid / Cylinder
h $\frac{\text { Volume }}{\text { Area of base }}$
Cone.h $\frac{3 \text { Volume }}{\text { Area of base }}$

Area of 4 walls $=2(l+b) h$

If, $V=S A$ of a sphere, then, $r=3$ and $d=6$

If 2 cylinder / cone

Equal volumes

$$
\begin{aligned}
& \frac{h_{1}}{h_{2}} \quad{\frac{r_{2}}{r_{1}}}^{2} \\
& \frac{r_{1}}{r_{2}} \quad \sqrt{\frac{h_{2}}{h_{1}}}
\end{aligned}
$$

Ratio of volume is given

$$
\begin{array}{lll}
\frac{h_{1}}{h_{2}} & \frac{r_{2}}{r_{1}} & \frac{v_{1}}{v_{2}} \\
\frac{r_{1}}{r_{2}} & \sqrt{\frac{h_{2}}{h_{1}}} & \frac{v_{1}}{v_{2}}
\end{array}
$$

$\bullet \quad$ Diagonal of cube $=\sqrt{3} \quad a[\mathrm{a}=$ side $]$
$-\quad$ Diagonal of a cuboid $=\sqrt{l^{2} \quad b^{2} \quad h^{2}}$

## (Chapter-11)

## Surface Area And Volume

1. An underground water tank is in the shape of cube of side 7 m . What will be its volume?
2. What will be volume of a box whose length 16 m , breadth 8 m and height is 5 m ?
3. The length, breadth and height of a room are $12 \mathrm{~m}, 10 \mathrm{~m}$, and 9 m respectively. Find the area of four walls of room?
4. The volume of a cube is $27 a^{3}$. Find the length of its edge?
5. How much Aluminium sheet will be required to make a container with lid whose length is 13 m , breadth is 8 m and height is 4 m ?
6. The volume of a cube is $1331 \mathrm{~cm}^{3}$. Find the length of its edge?
7. The length of diagonal of a cube is 17.32 cm . Find the volume of that cube?
8. Three cubes whose sides are $6 \mathrm{~cm}, 8 \mathrm{~cm}$ and 10 cm . They are melted and form a cube. Find the volume of that cube?
9. Two cubes have edge 10 m . Their edges have been joined and form a cuboid. What will be the surface area of cuboid thus formed?
10. The total volume of a cube is 512 cubic cm . Find the side of a cube?
11. A rectangular box 14 cm long, 10 cm wide and 5 cm high is to be made with card-board. Find the area of card-board to make that box?
12. What will be the volume of a cylindrical tank whose radius is 7 cm and height is 5 cm ?
13. How many solid spheres of $\frac{2}{3} \mathrm{~cm}$ radius can be made from a solid sphere of 2 cm radius?
14. If the volume and surface area of a sphere is numerically same then what will be its radius?
15. The volume of a right circular cylinder is $392 \pi \mathrm{~cm}^{3}$ and its height is 8 cm . Find the radius?
16. The surface area of a sphere is $448 \pi \mathrm{~cm}^{2}$. Find its radius?
17. What will be the edge of a cube? If its surface area is 324 sq cm .
18. The volume of a hemisphere is $144 \pi \mathrm{~cm}^{3}$. What will be its radius?
19. The curved surface area of a cone is $140 \pi \mathrm{~cm}^{2}$. What will be the radius of cone whose slant height is 5 cm .
20. The radius of a solid sphere is 12 cm . How many sphere can be made from it of 6 cm radius?
21. The volume of a cuboid is $840 \mathrm{~cm}^{3}$. If its length is 14 cm and breadth is 5 cm . Find the height of cuboid?
22. Four equal cubes have side 5 cm each. They are joined together edge to edge. What will be the surface area of cuboid thus formed?
23. The area of a rhombus is $56 \mathrm{~cm}^{2}$ and its diagonal is 7 cm . Find the length of other diagonal of the rhombus?
24. Find the maximum length of the rod that can be kept in cyboidal box of sides $30 \mathrm{~cm}, 24 \mathrm{~cm}$ and 18 cm .
25. The curved surface area of a cylinder is $216 \pi$. If its height is 18 cm then what will be its radius?
26. 60 circular plates of equal radius are placed on each other to form a cylinder. Find height of cylinder if thickness of each plate if $3 / 4 \mathrm{~cm}$.
27. Curved surface area of a cone is thrice and curved surface area of the other. Slant height of second cone is thrice the slant height of first. Find ratio of their radii.
28. A well of 2 m diameter is dug 14 m deep on the ground. Find the volume of earth taken out.
29. Volume of a solid sphere is $36 \pi \mathrm{~cm}^{3}$. Find its radius.
30. A boy recasted a cone of 4 cm height and 27 cm radius into a solid sphere. Find the radius of the sphere.

## Surface Area And Volume (Chapter-11) <br> Answers

1. $343 \mathrm{~m}^{3}$
2. $640 \mathrm{~m}^{3}$
3. $396 \mathrm{~m}^{2}$
4. 3 a
5. $376 \mathrm{~m}^{2}$
6. 11 cm
7. $1000 \mathrm{~cm}^{3}$
8. $1728 \mathrm{~cm}^{3}$
9. $1000 \mathrm{~m}^{2}$
10. 8 cm
11. $520 \mathrm{~cm}^{2}$
12. $770 \mathrm{~cm}^{2}$
13. 27
14. 3 units
15. 7 cm
16. $\sqrt{112} \mathrm{~cm}$ or $4 \sqrt{7} \mathrm{~cm}$
17. 9 cm
18. 6 cm
19. 28 cm
20. 8
21. 12 cm
22. $450 \mathrm{~cm}^{2}$
23. 16 cm
24. $\sqrt{1800} \mathrm{~cm}$ or $30 \sqrt{2} \mathrm{~cm}$
25. 6 cm
26. 45 cm
27. $9: 1$
28. $44 m^{3}$
29. 3 cm
30. 9 cm

## (Chapter-12)

## Statistics

- Mean $=\frac{\text { Sum of observations }}{\text { number of observations }}$
- Median :-

If ' $n$ ' is odd number median $=\frac{n+1}{2}{ }^{\text {th }}$ term
If ' $n$ ' is even number median $=\frac{\frac{\frac{n}{2}^{\text {th }} \text { term } \frac{n}{2} 1 \text { term }}{2}}{2}$

Mode : the mode is most frequently occuring observation

Sum of first n natural numbers $=\frac{n\left(\begin{array}{ll}n & 1\end{array}\right)}{2}$
$1^{2}+2^{2}+$ $\qquad$ $+n^{2}$
Sum of squares of first n natural numbers $=\frac{n\binom{n \quad 1)(2 n ~ 1)}{6} .}{}$
$\bullet \quad 1^{3}+2^{3}+\ldots--\ldots+n^{3}$
Sum of cubes of first ' $n$ ' natural numbers $=\frac{n(n-1)}{2}{ }^{2}$

## (Chapter-12)

## Statistics

1. For the class interval 21-25, what is the upper limit?
2. What is the class mark for the class interval 18-26?
3. What is the range for the given data :$31,32.5,20.3,27.9,28,19.7,31.7$.
4. If the Tally marks of a given data is $H H|||\mid$ then what is its frequency.
5. Given below is the no. of goals made by a team in 10 matches :-
$2,3,5,4,0,1,3,3,4$, 3
Find the mean.
6. Find the median for the above Q. 5
7. $2,3,4,5,0,1,3,3,4,3$ find the mode for the given data.
8. Find the mode for the data given below :-
$14,25,14,28,18,17,14,23,22,14,18$.
9. If the mean of $6,8,5,7, x$ and 4 is 7 then find the value of $x$.
10. If the mean for 10 observations is 20 and mean for other 15 observation is 16 then find the mean for all 25 observations.
11. Find the mean for:-
$4,3,7,0,0,6,8$.
12. Find the mode for the following :$7,9,12,13,7,12,15,7,12,7,25,18,7$.
13. The mean for three nos. is 6 . If two of them are $5 \& 8$ respectively then find the third number.
14. If means of $x_{1}, x_{2}$ is 6 and mean of $x_{1}, x_{2}$ and $x_{3}$ is 7 then find $x_{3}$.
15. Find the mean of first three natural numbers.
16. If 3 is the mean for $x, 3,4,5$ then find the value of $x$.
17. Find the mean for first three whole numbers.
18. What is the mean of $p, q$ and $r$.
19. The mean of $4,4,3,5,6,2$, is $\qquad$ .
20. One student has scored the marks in five subject as below :$70,64,56,54,51$. find the mean.
21. For which value of $p$, the data given below has mode 5 . $1,2,5,7,5,2,7,5,9,2,3, p, 11$
22. Find the median :-

36, 39, 42, 48, 52, 68, 69, 71, 72, 78.
23. The class marks are given below :-
$47,52,57,62,67,72,77,82$
What is the class size?
24. Find the class limit for the first class marks of above Q .
25. What is the range of $40,42,80,69,56,47 ?$

## Statistics (Chapter-12) <br> Answers

1. 25
2. 22
3. 12.8
4. 9
5. 2.8
6. 3
7. 3
8. 14
9. 12
10. 17.6
11. 4
12. 7
13. 5
14. 9
15. 2
16. 0
17. 1
18. $\frac{p+q+r}{3}$
19. 4
20. 59
21. 5
22. 60
23. 5
24. 44.5-49.5
25. 40

## (Chapter-13)

## Probability

- Probability $\mathrm{P}(\mathrm{E})$ of an event E is given by :-
$P(E) \quad \frac{\text { Number of trials in which } \mathrm{E} \text { has happened }}{\text { Total number of trials }}$
- The probability of an event lies between 0 and $1[(0$ and 1$)$ inclusive] $=0 \quad P(E) \quad 1$
- The probability of a sure event is 1
- The probability of an impossible event is 0 .

The sum of the probabilities of all the elementary events of an experiment is 1

For any event E,
$P(E) \quad P(\bar{E}) \quad 1$
where $\bar{E}$ stands for (not $E$ ).

## (Chapter-13)

## Probability

1. A coin is tossed once, find the probability of getting 'Head'?
2. In a pack of 52 cards what is the probability of getting a face card?
3. A dice is tossed once find the probability of getting a 'prime number'
4. A dice is tossed once find the probability of getting a number less than 5 .
5. In a pack of 52 cards find the probability of getting two of spades.
6. In a cricket match, a batsman hits a boundary of 5 times out of 30 balls he plays. Find the probability that he did not hit a boundary.
7. In a bag there are 5 white, 4 black, 3 red balls. One ball is picked up randomly what is the probability of getting a black ball?
8. A coin is tossed 500 times with following frequencies :Head -245 , Tail -255 . What is the probability of getting head?
9. In 250 consecutive days weather forecasts were correct 175 times. Find the probability of getting 'not correct' forecast?
10. In class IX total students were 36. Out of which 20 students are boys. Find the probability of girls in the class?
11. Between 5 and 15 numbers find the probability of having an odd number.
12. In 1500 families, 814 families have 2 children and rest of families have 1 child. Find the probability of families having 1 child?
13. In word 'INDIA' what is the probability of getting letter 'I'?
14. In a bag of 56 apples, 19 were rotten. One apple is chosen at random. Find the probability of getting a fresh apple?
15. A dice is tossed once, what is the probability of getting number '7'?
16. In a bag there are 5 white, 6 black and 3 green cards. One card is drawn at random. What is the probability of having a card which is not green?
17. In a class of 50 students $70 \%$ were passed. What is the probability of a failing child?
18. In a football team wining possibility is 0.4 . What is probability of loosing the game?
19. In a pack of 52 cards what is the probability of getting a red king?
20. In a locality there are 67 vehicles. In which 39 are black. What is the probability of a vehicle which is not black?
21. A survey of 250 students was conducted about the subject 'Statistics'. In which 143 students like statistics. Find the probability of a students who does not like statistics?
22. In word 'CLASSES'. What is the probability of getting letter 'S'?
23. In a class of 47 students, 29 students studies Home Science and rest students studies Drawing. Find the probability of Drawing students?
24. In word 'MATHEMATICS'. What is the probability of a vowel?
25. Between $1-70$, what is the probability of numbers which are divisible by '7'?

## Probability (Chapter-13) <br> Answers

1. $\frac{1}{2}$
2. $\frac{3}{13}$
3. $\frac{1}{2}$
4. $\frac{2}{3}$
5. $\frac{1}{52}$
6. $\frac{5}{6}$
7. $\frac{1}{3}$
8. $\frac{49}{100}$
9. $\frac{3}{10}$
10. $\frac{4}{9}$
11. $\frac{4}{9}$
12. $\frac{343}{750}$
13. $\frac{2}{5}$
14. $\frac{37}{56}$
15. 0
16. $\frac{11}{14}$
17. $\frac{3}{10}$
18. 0.6
19. $\frac{1}{26}$
20. $\frac{28}{67}$
21. $\frac{107}{250}$
22. $\frac{3}{7}$
23. $\frac{18}{47}$
24. $\frac{4}{11}$
25. $\frac{9}{68}$.
