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## UNIT 13

## $10^{\mathrm{th}}$ STATISTICS AND PROBABILITY

Statistics are the only tools by which an opening can be cut through the formidable thicket of difficulties that bars the path of those who pursue the Science of Man.

1. Marks obtained by 70 students are given below:

| Marks | 20 | 70 | 50 | 60 | 75 | 90 | 40 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of <br> Students | 8 | 12 | 18 | 6 | 9 | 5 | 12 |

Find the median.
Ans:

| Marks | No . of <br> students | c.f |
| :--- | :--- | :--- |
| 20 | 8 | 8 |
| 40 | 12 | 20 |
| 50 | 18 | 38 |
| 60 | 6 | 44 |
| 70 | 12 | 53 |
| 75 | 9 | 58 |
| 90 | 5 | 70 |

$$
\mathrm{N}=70
$$

$$
\frac{N}{2}=
$$

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2. The sum of deviations of a set of values $x_{1}, x_{2}, x_{3}, \ldots \ldots \ldots . x_{n}$, measured from 50 is -10 and the sum of deviations of the values from 46 is 70 .
Find the value of $n$ and the mean.
(Ans:20,.49.5)
Ans: We have

$$
\begin{align*}
& \sum_{i=1}^{n}\left(X_{i}-50\right)=-10 \text { and } \sum_{i=1}^{n}\left(X_{i}-46\right)=70 \\
& \sum_{i=1}^{n} X_{i}-50 \mathrm{n}=-10 \quad \ldots \ldots \ldots .(1)  \tag{1}\\
& \text { and } \sum_{i=1}^{n} X_{i}-46_{\mathrm{m}}=70 \ldots \ldots \ldots \ldots \text { (2) } \tag{2}
\end{align*}
$$

subtracting (2) from (1), we get
$-4 \mathrm{n}=-80$ we get $\mathrm{n}=20$
$\sum_{i=1}^{n} X_{i}-50 \times 20=-10$
$\sum_{i=1}^{n} X_{i}=990$
Mean $=\frac{1}{n}\left(\sum_{i=1}^{n} X_{i}\right)=\frac{990}{20}=49.5$
hence $\mathrm{n}=20$ and mean $=49.5$
3. Prove that $\sum\left(x_{i}-\bar{x}\right)=0$

Ans: $\quad$ To prove $\sum^{\text {in }}\left(\hat{X}_{i}-\bar{X}\right)=0$ algebraic sum of deviation from mean is zero

$$
\text { We have, } \bar{X}=\frac{1}{n}\left(\sum_{i=1}^{n} X_{i}\right)
$$

h $\bar{X}=\sum_{i=1}^{n} X_{i}$
Now, $\sum_{i=1}^{n}\left(X_{i}-\bar{X}\right)=\left(\mathrm{X}_{1}-\bar{X}\right)+\left(\mathrm{X}_{2}-\bar{X}\right)+\ldots \ldots \ldots+\left(\mathrm{X}_{\mathrm{n}}-\bar{X}\right)$

$$
\begin{aligned}
& \sum_{i=1}^{n}\left(X_{i}-\bar{X}\right)=\left(\mathrm{X}_{1}+\mathrm{X}_{2}+\ldots \ldots \ldots+\mathrm{X}_{\mathrm{n}}\right)-\mathrm{n} \bar{X} \\
& \sum_{i=1}^{n}\left(X_{i}-\bar{X}\right)=\sum_{i=1}^{n} X_{i}-\mathrm{n} \bar{X} \\
& \sum_{i=1}^{n}\left(X_{i}-\bar{X}\right)=\mathrm{n} \bar{X}-\mathrm{n} \bar{X}
\end{aligned}
$$

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$$
\begin{aligned}
& \sum_{i=1}^{n}\left(X_{i}-\bar{X}\right)=0 \\
& \text { Hence, } \sum_{i=1}^{n}\left(X_{i}-\bar{X}\right)=0
\end{aligned}
$$

4.Compute the median from the following data

| Mid value | 115 | 125 | 135 | 145 | 155 | 165 | 175 | 185 | 195 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 6 | 25 | 48 | 72 | 116 | 60 | 38 | 22 | 3 |

Ans: Here, we are given the mid values. So, we should first find the upher and lower limits of the various classes. The difference between two consecutive values is $\mathrm{h}=125-115=10$
$\therefore$ Lower limit of a class $=$ Midvalue $-\mathrm{h} / 2$
Upper limit $=$ Midvalue + h $/ 2$
Calculate of Median

| Mid - value | Class Groups | Frequency | Cumulative <br> frequency |
| :--- | :--- | :--- | :--- |
| 115 | $110-120$ | 6 | 6 |
| 125 | $120-130$ | 25 | 31 |
| 135 | $130-140$ | 48 | 79 |
| 145 | $140-150$ | 72 | 151 |
| 155 | $150-160$ | 116 | 267 |
| 165 | $160-170$ | 60 | 327 |
| 175 | $170-180$ | 38 | 365 |
| 185 | $180-190$ | 22 | 387 |
| 195 | $190-200$ | 3 | 390 |
|  |  |  | $\mathrm{~N}=\Sigma \mathrm{f}_{\mathrm{i}}=390$ |

We have,
$\mathrm{N}=390$
$\therefore \mathrm{N} / 2=390 / 2=195$

The cumulative frequency first greater than N i.e. 195 is 267 and the corresponding class is $150-160$, so, $150-160$ is the median class.
$\mathrm{L}=150, \mathrm{f}=116, \mathrm{~h}=10, \mathrm{f}=151$

Now,

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$$
\begin{gathered}
\text { Median }=\mathrm{L}+\frac{\frac{n}{2}-f}{f} \times \mathrm{h} \\
\text { Median }=150+\frac{195-151}{116} \times 10=153.8
\end{gathered}
$$

5. The mean of ' $n$ ' observation is $\bar{x}$, if the first term is increased by 1 , second by 2 and so on. What will be the new mean.

Ans: $\quad$ I term +1
II term +2
III term +3
n term +n
6. In a frequency distribution mode is 9.88 , mean is 8.32 find the median. (Ans: 8.17)

Ans: $\quad$ Mode $=3$ median -2 mean
$7.88=3$ median $-2 \times 8.32$
$7.88+16.64=3$ median
$\frac{24.52}{3}=$ médian
$\therefore$ median $=8.17$
7. The mode of a distribution is $55 \&$ the modal class is $45-60$ and the frequency preceding the modal class is 5 and the frequency after the modal class is 10 .Find

- the frequency of the modal class.
(Ans:15)
Ans: mode $=55$
alodal class $=45-60$
Modal class preceding $f_{1}=5$
After the modal class $=\mathrm{f}_{2}=10$

$$
\begin{aligned}
\text { Mode }=\mathrm{L}+\frac{f-f_{1}}{2 f-f_{1}-f_{2}} \times \mathrm{h} \\
55=45+\frac{f-5}{2 f-5-10} \times 15
\end{aligned}
$$

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$$
\begin{aligned}
& 10=\left(\frac{f-5}{2 f-15}\right) \times 15 \\
& \frac{10}{15}=\frac{f-5}{2 f-15} \\
& 20 \mathrm{f}-150=15 \mathrm{f}-75 \\
& 5 \mathrm{f}=75 \\
& \mathrm{f}=\frac{75}{5}= 15
\end{aligned}
$$

8. The mean of 30 numbers is 18 , what will be the new mean, if each observation is increased by 2 ?
(Ans:20)
Ans: Let $x_{1}, x_{2}, x_{3} \ldots \ldots x_{30}$ be 30 number with then mean equal to 18 then

$$
\begin{aligned}
\bar{X} & =\frac{1}{n}\left(\sum x_{i}\right) \\
18 & =\frac{x_{1}+x_{2}+x_{3} \ldots \ldots+x_{30}}{30}
\end{aligned}
$$

$$
\mathrm{x}_{1}+\mathrm{x}_{2}+\mathrm{x}_{3+\ldots \ldots}+\mathrm{x}_{30}=18 \times 30=540
$$

New numbers are $x_{1}+2, x_{2},+2 x_{3}+3 \backsim x_{30}+2$
Let $\bar{X}$ be the mean of new numbers
then $\bar{X}=\frac{\left(x_{1}+2\right)+\left(x_{2}+2\right)+\square+\left(x_{30}+2\right)}{30}$


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9. In the graphical representation of a frequency distribution if the distance between mode and mean is k times the distance between median and mean then find the value of k .
(Ans:k=3)

## Self Practice

10. Find the mean of 30 numbers given mean of ten of them is 12 and the mean of remaining 20 is 9 .
(Ans:10)

Ans: Total number of mean $=30$
Mean of 10 is $=12$

$$
12=\frac{\sum_{i=1}^{n} X_{i}}{10}
$$

$$
\begin{equation*}
\sum \mathrm{X}_{\mathrm{i}}=12 \times 10=120 \tag{1}
\end{equation*}
$$

Mean of 20 numbers is $=9$

$$
9=\frac{\sum X_{i}}{20}
$$

$$
\begin{equation*}
9 \times 20=\sum_{i=1}^{n} X_{i} \tag{2}
\end{equation*}
$$

$$
180==\sum \mathrm{X}_{\underline{i}}
$$

(1) $+(2)$

Mean of 20 numbers $=\frac{120+180}{30}$

$$
=\frac{300}{30}=10
$$

