PRE-BOARD SAMPLE PAPER 2018-19

## CLASS-X

## BLUEPRINT



# JSUIIL THOBIRL ACBSE Coaching for O(Aathematics and Science 

## PRE BOARD SAMPLE PAPER 2018-19

# CLASS-X <br> <br> MATHEMATICS 

 <br> <br> MATHEMATICS}

Maximum Marks: 80
Time: 3 HOURS
General Instructions:

1. All Questions are compulsory.
2. The question paper consists of 30 questions divided into four sections $A, B, C$ and $D$. Section - A comprises of 6 questions of 1 mark each, Section - B comprises of 6 questions of 2 mark each, Section - C comprises of 10 questions of 3 mark each and Section - D comprises of 8 questions of 4 mark each.
3. Use of calculator is not permitted.
4. An additional 15 minutes time has been allotted to read this question paper only.

## SECTION- A

Q1. If $\alpha$ and $\beta$ are the zeroes of the quadratic polynomial $f(x)=x^{2}+2 x+1$, then find $\alpha+\beta$
Q2. $\triangle \mathrm{ABC}$ is such that $\mathrm{AB}=3 \mathrm{~cm}, \mathrm{BC}=2 \mathrm{~cm}, \mathrm{CA}=2.5 \mathrm{~cm}$. If $\triangle \mathrm{DEF} \sim \triangle \mathrm{ABC}$ and $\mathrm{EF}=4 \mathrm{~cm}$, then find perimeter of $\triangle \mathrm{DEF}$.

Q3. The height of a tower is $\sqrt{3}$ times of its shadow. Find the angle of elevation of the sun.
Q4. One die is tossed. Find the probability of getting a prime number.
Q. 5 Find the distance between points $\mathrm{A}(2,3)$ and $\mathrm{B}(4,1)$.

Q6. The length of a tangent from a point A at distance 5 cm from the centre of a circle is 4 cm , Find the radius of the circle?

## SECTION B

Q7. Use Euclid's Division Algorithm to find HCF of 870 and 225.
Q8. Find the value of k , so that the quadratic equation $\mathrm{kx}(\mathrm{x}-2)+6=0$, has two equal roots.
Q9. Find the value of $k$, so that the pair of linear equation has unique solution:

$$
2 x+k y=11 \text { and } x-2 y=-12
$$

Q10. Find the ratio in which the segment joining the points $(-3,10)$ and $(6,-8)$ is divided by $(-1,6)$
Q11. If $\tan 2 \mathrm{~A}=\cot \left(\mathrm{A}-18^{\circ}\right)$, then find the value of A .
Q12. The perimeter of the base of a cone is 44 cm and the slant height is 25 cm . Find the curved surface area of the cone?

## SECTION C

Q13. Show that $\sqrt{5}$ is irrational.
Q14. Find the zeroes of $6 x^{2}-3-7 x$, and verify the relationship between the zeroes and the coefficients. https://isuniltutorial.weebly.com/ Page |2

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Q15. Find a point on $x$-axis which is equidistant from the points $A(2,-5)$ and $B(-2,9)$.
Q16. Prove that the lengths of tangents drawn from an external point to a circle are equal.
Q17. Prove that $\sqrt{\frac{1+\sin x}{1-\sin x}}=\sec x+\tan x$

$$
\frac{\cos A}{1-\tan A}+\frac{\begin{array}{c}
\text { or } \\
\sin A
\end{array}}{1-\cot A}=\sin \mathrm{A}+\cos \mathrm{A}
$$

Q18. Evaluate: $\frac{\tan ^{2} 60^{\circ}+4 \sin ^{2} 45^{\circ}+3 \sec ^{2} 30^{\circ}+5 \cos ^{2} 90^{\circ}}{\operatorname{cosec} 30^{\circ}+\sec 60^{\circ}-\cot ^{2} 30^{\circ}}$
Q19. $\triangle \mathrm{ABC}$ is such that $L A D C=L B A C$. Prove that $\mathrm{CA}^{2}=\mathrm{CD} \times \mathrm{CD}$


Q20 If the mean of the following distribution is 50 find the value of p .

| Class | $0-20$ | $20-40$ | $40-60$ | $60-80$ | $80-100$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 17 | 28 | 32 | P | 19 |

Q21 From the top and foot of a tower 40m high, the angles of elevation of the top of a light house are found to be $30^{\circ}$ and $60^{\circ}$ respectively. Find the height of the light house. Also, find the distance of the top of the light house from the foot of the tower.
Q. 22 One card is drawn from a well-shuffled deck of 52 cards. Find the probability of getting
(i) a king of red colour
(ii) a face card
(iii) a red face card

## SECTION D

Q23. Represent the following system of equation graphically:

$$
2 x+y=2, \quad 2 y-x=4
$$

Shade the triangular region formed by the lines and the $x$-axis
Q24. The difference of squares of two numbers is 180 . The square of the smaller number is 8 times the larger number. Find the two numbers.

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Q25 If the sum of the first $n$ terms of an A.P. is $4 n-n^{2}$, what is the first term? What is the sum of first two terms? What is the second term? Find the $10^{\text {th }}$ term.
Q26. State and prove the converse of Pythagoras theorem.

## OR

Prove that the ratio of areas of two similar triangles is equal to the square of the ratio of their corresponding sides.
Q27. Draw a right triangle in which the sides (other than hypotenuse) are of lengths 4 cm and 3 cm . Then construct another triangle whose sides are $\frac{3}{5}$ times the corresponding sides of the given triangle.

Q28. For the data given below draw more than type ogive graph. Hence find its Median

| Marks | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number of students | 5 | 4 | 8 | 10 | 15 | 18 |

Q29. The area of an equilateral triangle is $17320.5 \mathrm{~cm}^{2}$ About each angular point as centre, a circle is described with radius equal to half the length of the side of the triangle. Find the area of the triangle not included in the circles. (Use $\pi=3.14$ and $\sqrt{3}=1.73205$ )

Q30. A container, opened from the top and made up of a metal sheet, is in the form of a frustum of a cone of height 16 cm with radii of its lower and upper ends are 8 cm and 20 cm , respectively. Find the cost of the milk which can completely fill the container, at the rate of Rs 20 per liter. Also find the cost of metal sheet used to make the container, if it cost Rs 8 per $100 \mathrm{~cm}^{2}$.

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CLASS X MATHS 2018-19<br>MARKING SCHEME<br>PRE BOARD SAMPLE PAPER

Q. $1 \alpha+\beta=-2$
Q. 2 perimeter $=15 \mathrm{~cm}$
Q. 3 Angle of elevation $=60^{\circ}$
Q. 4 Probability $=1 / 2$
Q. 5 distance $=2 \sqrt{ } 2$
Q. $6 \mathrm{r}=3 \mathrm{~cm}$
Q. $7870=225 \times 3+195$
$225=195 \times 1+30$
$195=30 \times 6+15$
$30=15 \times 2+0$
$\mathrm{HCF}=15$
Q. $8 \mathrm{KX}^{2}-2 \mathrm{KX}+6=0$
$4 \mathrm{~K}^{2}-24 \mathrm{~K}=0$
$4 \mathrm{k}(\mathrm{k}-6)=0$
$\mathrm{K}=6$
Q. 9 For correct condition

$$
\mathrm{k} \neq-4
$$

Q. 10 for correct formula and steps

Ratio=7:2
$\mathrm{Q} .11 \cot (90-2 \mathrm{~A})=\cot \left(\mathrm{A}-18^{\circ}\right)$
$90-2 \mathrm{~A}=\mathrm{A}-18$

1 Mark
1 Mark
1 Mark
1 Mark
1 Mark
1 Mark

1/2 Mark
½ Mark
1 Mark
1 Mark
1 Mark
1/2 Mark each
1 Mark
1/2 Mark
1/2 Mark
$A=36$
Q. $122 \pi \mathrm{r}=44$
$\mathrm{r}=7$
CSA $=\pi \mathrm{rl}$

$$
\begin{array}{l}\text { CSA }=550 \mathrm{~cm}^{2} \\ \text { Q. } 13 \text { For correct proof } \\ \text { Q. } 14 \alpha=-1 / 3 \& \beta=3 / 2 \\ \quad \alpha+\beta=7 / 6=-\mathrm{b} / \mathrm{a} \\ \alpha \beta=-1 / 2=\mathrm{c} / \mathrm{a}\end{array}
$$

Q. 15 Let the point on x -axis be $(\mathrm{x}, 0)$

For correct formula
Point is $(-9,0)$
Q. 16 For given

To prove
For correct figure
For correct proof
Q. 17 For correct proof
Q. 18 For correct values

For correct answer $=9$
Q. 19 In $\triangle \mathrm{ABC}$ and $\triangle \mathrm{DAC}$
$\angle \mathrm{BAC}=\angle \mathrm{ADC}$
$\angle \mathrm{C}=\angle \mathrm{C}$
$\triangle A B C \sim \triangle D A C(A A)$

1 Mark
$1 / 2$ Mark
½ Mark
½ Mark
½ Mark

3Marks
1 Mark
1 Mark
1 Mark
$1 / 2$ Mark
½ Mark
2 Mark
1/2 Mark
$1 / 2$ Mark
1/2 Mark
1½ Mark
3 Mark
2 Mark
1 Mark

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$$
\begin{aligned}
& \frac{C B}{C A}=\frac{C A}{C D} \\
& \Rightarrow C A^{2}=C B \times C D
\end{aligned}
$$

Q. 20 For correct table

$$
\text { mean }=\sum \mathrm{fixi} / \sum \mathrm{fi}=(4320+70 \mathrm{p}) / 96+\mathrm{p}=50
$$

$\mathrm{p}=24$
1 mark
1mark
1mark
1mark
$1 / 2$ mark
$1 / 2$ mark 1 mark

1/2 Mark
1/2mark
(ii)face card $=12$

Probability $12 / 52=3 / 12$
(iii)a red face card=6

Probability $=6 / 52=3 / 26$
Q. 23 for correct table
for correct graph
For correct shading
Q. $24 \mathrm{x}^{2}-\mathrm{y}^{2}=180$
$y^{2}=8 x$
$x^{2}-8 x-180=0$
$\tan 30=\mathrm{h} / \mathrm{x}$
$\tan 60=(40+\mathrm{h}) / \mathrm{x}$
$\sqrt{3} \mathrm{x}=40+\mathrm{h}$

$$
\mathrm{h}=20 \mathrm{~m} \text { and } \mathrm{x}=20 \sqrt{3} \mathrm{~m}
$$

Q.22(i)king of red colour $=2$

Probability $=$ no. of favourable outcome /no. of total outcome

$$
=2 / 52=1 / 26
$$

1mark

1mark
1 mark
2 mark
1 mark
1 mark
$1 / 2$ mark

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$$
x=-10, x=18
$$

numbers are $18 \& 12$
Q. $25 \quad \mathrm{Sn}=4 \mathrm{n}-\mathrm{n}^{2}$
$S_{1}=3$
$S_{2}=4$
$\mathrm{a}_{2}=\mathrm{S}_{2}-\mathrm{S}_{1}=1$
$\mathrm{a}_{10}=\mathrm{S}_{10}-\mathrm{S}_{9}=-15$
Q 26. For given
To prove
For figure
For construction
For proof
Q 27. For correct right triangle
For similar triangle
For steps of construction
Q 28.

| Marks obtained | No. of students |
| :--- | :--- |
| More than or equal to 10 | 60 |
| More than or equal to 20 | 55 |
| More than or equal to 30 | 51 |
| More than or equal to 40 | 43 |
| More than or equal to 50 | 33 |
| More than or equal to 60 | 18 |

For correct ogive
Median $=42.66$
$11 / 2$ mark
1 mark
$1 / 2$ mark
$1 / 2$ mark
1 mark
2 mark
$1 / 2$ mark
$1 / 2$ mark
$1 / 2$ mark
$1 / 2$ mark
2 marks
1 mark
2 marks
1 mark
1 mark for the table

2 marks
1 mark

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Q29).

Area of a $\Delta=17320.5 \mathrm{~cm}^{2}$
$\Rightarrow \sqrt{ } 3 / 4$ side $^{2}=17320.5$
$\Rightarrow$ side $^{2}=173205 / 10$ X $4 / \sqrt{ } 3$

$$
=173205 / 10 \times 4 / 1.73205
$$

Side $=2 \mathrm{X} 100=200 \mathrm{~cm}$.
1 Mark
$\therefore$ radius $=200 / 2=100 \mathrm{~cm}$.
$\therefore$ Area of shaded portion $=$ area of $\Delta-3 \mathrm{x}$ area of sectors

$$
\begin{aligned}
& =17320.5-3 \times(60 / 360 \times 3.14 \times 100 \times 100) \\
& =17320.5-15700 \\
& =1620.5 \mathrm{~cm}^{2}
\end{aligned}
$$

Q30. Here $\mathrm{h}=16 \mathrm{~cm} ; \mathrm{r}=20 \mathrm{~cm} ; \mathrm{R}=8 \mathrm{~cm}$

Cost of milk = Rs 209 (approx)
Surface area of frustum shaped container open at the top $=\pi(r+r) l+\pi r^{2}=1959.36 \mathrm{~cm}^{2} \quad 1$
Cost of metal sheet $=1959.36 \times 8 / 100=$ Rs 156.75

