## JSUNIL TUTORIAL, SAMASTIPUR By Jsunil

## Class 10 Chapter: Application of Trigonometry [Hight and Distance] Solved Problems

Question: A kite is flying with a string of length 200 m. If the thread makes an angle 30° with the ground, find the distance of the kite from the ground level. (Here, assume that the string is along a straight line)

*Solution* Let *h* denote the distance of the kite from the ground level.



Thus, the angular elevation of the Sun from the ground level is 60°.

Question: The angle of elevation of the top of a tower as seen by an observer is 30°. The observer is at a distance of  $30\sqrt{3}$  m from the tower. If the eye level of the observer is 1.5 m above the ground level, then find the height of the tower.

*Solution* Let *BD* be the height of the tower and *AE* be the distance of the eye level of the observer from the ground level.

Draw *EC* parallel to *AB* such that AB = EC. Given  $AB = EC = 30\sqrt{3}$  m and AE = BC = 1.5 m





Hence, the height of the hill is 150 m.

Question: A vertical wall and a tower are on the ground. As seen from the top of the tower, the angles of depression of the top and bottom of the wall are 45° and 60° respectively. Find the height of the wall if the height of the tower is 90 m. (use  $\sqrt{3} = 1.732$ )

Let AE denote the wall and BD denote the tower. Solution 73 S. Draw *EC* parallel to *AB* such that AB=EC. Thus, AE=BC. *u*-06 Let AB = x metres and AE = h metres. 90 m 45° E C Given that BD = 90 m and  $\angle DAB = 60^\circ$ ,  $\angle DEC = 45^\circ$ . Now. AE = BC = h metres 60° Thus, CD = BD - BC = 90 - h. B A x In the right angled  $\triangle DAB$ ,  $\tan 60^\circ = \frac{BD}{AB} = \frac{90}{x}$ Fig. 7.14  $\implies x = \frac{90}{\sqrt{3}} = 30\sqrt{3}$ (1)In the right angled  $\triangle DEC$ ,  $\tan 45^\circ = \frac{DC}{EC} = \frac{90 - h}{x}$ x = 90 - hThus. (2)From (1) and (2), we have  $90 - h = 30\sqrt{3}$ 

Thus, the height of the wall,  $h = 90 - 30\sqrt{3} = 38.04 \,\mathrm{m}$ 

- Question: A girl standing on a lighthouse built on a cliff near the seashore, observes two boats due East of the lighthouse. The angles of depression of the two boats are 30° and 60°. The distance between the boats is 300 m. Find the distance of the top of the lighthouse from the sea level.
  - *Solution* Let *A* and *D* denote the foot of the cliff and the top of the lighthouse respectively. Let *B* and *C* denote the two boats.

Let *h* metres be the distance of the top of the lighthouse from the sea level.

Let AB = x metres. Given that  $\angle ABD = 60^\circ$ ,  $\angle ACD = 30^\circ$ 

In the right angled  $\triangle ABD$ ,

 $\tan 60^\circ = \frac{AD}{AB}$  $\implies AB = \frac{AD}{\tan 60^\circ}$  $x = \frac{h}{\sqrt{2}}$ 



Thus,

Also, in the right angled  $\triangle ACD$ , we have

$$\tan 30^{\circ} = \frac{AD}{AC}$$

$$\implies AC = \frac{AD}{\tan 30^{\circ}} \implies x + 300 = \frac{h}{\left(\frac{1}{\sqrt{3}}\right)}$$
Thus,  $x + 300 = h\sqrt{3}$ .  
Using (1) in (2), we get  $\frac{h}{\sqrt{3}} + 300 = h\sqrt{3}$   
 $\implies h\sqrt{3} - \frac{h}{\sqrt{3}} = 300$   
 $\therefore \qquad 2h = 300\sqrt{3}$ . Thus,  $h = 150\sqrt{3}$ .

(1)

Hence, the height of the lighthouse from the sea level is  $150\sqrt{3}$  m.

Question: A boy spots a balloon moving with the wind in a horizontal line at a height of 88.2 r from the ground level. The distance of his eye level from the ground is 1.2 m. The angle o elevation of the balloon from his eyes at an instant is 60°. After some time, from the sam point of observation, the angle of elevation of the balloon reduces to 30°. Find the distance covered by the balloon during the interval.

*Solution* Let *A* be the point of observation.

Let *E* and *D* be the positions of the balloon when its angles of elevation are  $60^{\circ}$  and  $30^{\circ}$  respectively.

Let *B* and *C* be the points on the horizontal line such that BE = CD.

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Question: A flag post stands on the top of a building. From a point on the ground, the angles of elevation of the top and bottom of the flag post are 60° and 45° respectively. If the height of the flag post is 10 m, find the height of the building. (use  $\sqrt{3} = 1.732$ )

## Solution

Let *A* be the point of observation and *B* be the foot of the building.

Let BC denote the height of the building and CD denote height of the flag post.

Given that  $\angle CAB = 45^\circ$ ,  $\angle DAB = 60^\circ$  and CD = 10 m

Let BC = h metres and AB = x metres.

Now, in the right angled  $\triangle CAB$ ,

tan 
$$45^\circ = \frac{BC}{AB}$$
.  
Thus,  $AB = BC$  i.e.,  $x = h$ 

חס

DC

Also, in the right angled  $\triangle DAB$ ,

$$\tan 60^\circ = \frac{BD}{AB}$$
$$AB = \frac{h+10}{\tan 60^\circ} \implies x = \frac{h+10}{\sqrt{3}}$$



(1)

(2)

From (1) and (2), we get  $h = \frac{h+10}{\sqrt{3}}$ 

$$\implies \sqrt{3} h - h = 10$$
  
$$\implies h = \left(\frac{10}{\sqrt{3} - 1}\right) \left(\frac{\sqrt{3} + 1}{\sqrt{3} + 1}\right) = \frac{10(\sqrt{3} + 1)}{3 - 1}$$
  
$$= 5(2.732) = 13.66 \text{ m}$$

Hence the height of the building is 13.66 m



Question: The angle of elevation of an aeroplane from a point A on the ground is 60°. After a flight of 15 seconds horizontally, the angle of elevation changes to 30°. If the aeroplane is flying at a speed of 200 m/s, then find the constant height at which the aeroplane is flying.

*Solution* Let A be the point of observation.



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