- 1. Factorise a. (i)  $a^3 + 27b^3 + 8c^3 - 18abc$  (ii)  $a^6 + 4a^3 - 1$ (iii)  $1331a^3 + 125b^3 - 8c^3 + 330abc$ b. (iv)  $343x^3 - 8y^3 - 125z^3 - 210xyz$  (v)  $p - q^3 + q - r^3 + r - p^3$  $x - a^{3} + x - b^{3} + x - c^{3} - 3 x - a x - b x - c$  given 3x = a + b + c2. Evaluate 3. Find remainder using remainder theorem a. (i)  $x^3 + x^2 - 2x + 1 \div x - 3$  (ii)  $x^3 - 9x^2 + 45x - 63 \div x - 2$ (iii)  $x^3 - 12x^2 + 11x - 5 \div 2x - 1$ 4. Using factor theorem show (i) x = 3 is a factor of  $x^3 + x^2 = 17x + 15$ 5. (ii)Using factor theorem show x - 2 is a factor of  $x^6 - 64$ 6. Factorise using factor theorem a.  $2x^3 + 7x^2 - 9$  (ii)  $4z^3 + 23z^2 - 41x - 42$  (iii)  $6x^3 - x^2 - 12x - 5$ 7. (iv)  $6x^2 - 13x + 6$  (v)  $p^3(q - r)^3 + q^3(r - p)^3 + r^3(p - q)^3$ 8. Find value using suitable identity 9. (a)  $999^{3}$  (b)  $99.8^{3}$  (c)  $x^{3} - 8y^{3} - 36xy - 216$  when x = 2y + 6.(d)  $70^{3} - 50^{3} - 20^{3}$ 10.  $x^{3} + y^{3} + z^{3} - 3xyz = (x + y + z)[(x - y)^{2} + (y - z)^{2} + (z - x)^{2}]$ 11. Find the remainder when  $x^3 - 5x + 8$  is divided by x - 212. Find m if x - 3 is a factor of  $x^3 + x^2 - mx + 15$ 13. Find dimensions of a Cuboid if its volume is  $15ax^2 + 10ax - 25a$ 14. Factorise:  $2x^2 + 3y^2 + 8z^2 - 2\sqrt{6}xy - 4\sqrt{6}yz + 8zx$ 15.  $x = \frac{1}{2}\sqrt{3}$ , then find  $x + \frac{1}{x}$ 16. If  $27^x = \frac{9}{3^x}$ , find the value of x. 17. 15. Factorise a)  $x^9 - y^9$ b)  $x^6 - 7x^3 - 8$ 18. 16. Find value of 'a' for which (x - 4) is a factor of  $(2x^3 - 3x^2 - 18x + a)$ . 19. 17. Find the constant k if 2 x -1 is a factor of  $f(x) = 4 x^2 + kx + 1$ . Using this value of k, factorize f(x)completely. 20. 18. The expression  $2x^3 + ax^2 + bx - 2$  leaves remainders of 7 and 0 when divided by 2x - 3 and x + 2respectively. Calculate the values of a and b. With these values of a and b, factories the expression completely. 21. 19. If x +1 and x -1 are factors of  $f(x) = x^3 + 2ax + b$ , calculate the values of a and b. Using these values of a and b, factories f(x) completely. 22. 20. If  $x^2$  -1 is a factor of  $f(x) = x^4 + ax + b$ , calculate the values of a and b. Using these values of a and b, factories f(x). 23. 21. Given that  $x^2 - x - 2$  is a factor of  $x^3 + 3x^2 + ax + b$ , calculate the values of a and b and hence find the remaining factor. 24. 22. The polynomial  $x^4$  +bx<sup>3</sup> +59 x<sup>2</sup> +cx +60 is exactly divisible by x<sup>2</sup> +4 x +3. Find the values of b and c.
- 25. Show that x -1 is a factor of 2  $x^2 + x$  -3. Hence factories 2  $x^2 + x$  -3 completely.
- 26. Show that  $2 \times +3$  is a factor of  $6 \times^2 +5 \times -6$ . Hence find the other factor.
- 27. Show that x +2 is a factor of  $f(x) = x^3 + 2x^2 x 2$ . Hence factorise f(x) completely.
- 28. Show that x -1 is a factor of  $x^5$  -1 while  $x^5$  +1 is not divisible by x -1.
- 29. Using remainder theorem, find the value of a if the division of x<sup>3</sup> +5 x<sup>2</sup> -ax +6 by (x -1) leaves the remainder 2