

10th Trigonometry Identities

Evaluate the following:

1. $\frac{\cot 54^\circ}{\tan 36^\circ} + \frac{\tan 20^\circ}{\cot 70^\circ} - 2$

2. $\sec 50^\circ \sin 40^\circ + \cos 40^\circ \operatorname{cosec} 50^\circ$

3. $\frac{\cos 80^\circ}{\sin 10^\circ} + \cos 59^\circ \operatorname{cosec} 31^\circ$

4. $2 \frac{\cos 67^\circ}{\sin 23^\circ} - \frac{\tan 40^\circ}{\cot 50^\circ} - \sin 90^\circ$

5. $2 \frac{\sin 43^\circ}{\cos 47^\circ} - \frac{\cot 30^\circ}{\tan 60^\circ} - \sqrt{2} \sin 45^\circ$

6. $\sin(50^\circ + \theta) - \cos(40^\circ - \theta)$

7. $\frac{\cot 40^\circ}{\tan 50^\circ} - \frac{1}{2} \left(\frac{\cos 35^\circ}{\sin 55^\circ} \right)$

8. $\frac{\cos 75^\circ}{\sin 15^\circ} + \frac{\sin 12^\circ}{\cos 78^\circ} - \frac{\cos 18^\circ}{\sin 72^\circ}$

9. $\frac{\cos 35^\circ}{\sin 55^\circ} + \frac{\sin 11^\circ}{\cos 79^\circ} - \cos 28^\circ \operatorname{cosec} 62^\circ$

10. $\tan 35^\circ \tan 40^\circ \tan 45^\circ \tan 50^\circ \tan 55^\circ$

11. $\tan 7^\circ \tan 23^\circ \tan 60^\circ \tan 67^\circ \tan 83^\circ$

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12. $\tan 5^\circ \tan 25^\circ \tan 30^\circ \tan 65^\circ \tan 85^\circ$

13. $\operatorname{cosec}(65^\circ + \theta) - \sec(25^\circ - \theta) - \tan(55^\circ - \theta) + \cot(35^\circ + \theta)$

14. $\frac{\tan 50^\circ + \sec 50^\circ}{\cot 40^\circ + \operatorname{cosec} 40^\circ} + \cos 40^\circ \operatorname{cosec} 50^\circ$

15. $\frac{\cos^2 20^\circ + \cos^2 70^\circ}{\sin^2 59^\circ + \sin^2 31^\circ}$

16. $\frac{\cos^2 20^\circ + \cos^2 70^\circ}{\sin^2 20^\circ + \sin^2 70^\circ} + \sin^2 64^\circ + \cos 64^\circ \sin 26^\circ$

17. $\frac{\sin 220^\circ + \sin^2 70^\circ}{\cos^2 20^\circ + \cos^2 70^\circ} + \left(\frac{\sin(90^\circ - \theta) \sin \theta}{\tan \theta} + \frac{\cos(90^\circ - \theta) \cos \theta}{\cot \theta} \right)$

18. $\frac{\sec(90^\circ - \theta) \operatorname{cosec} \theta - \tan(90^\circ - \theta) \cot \theta + (\cos^2 35^\circ + \cos^2 55^\circ)}{\tan 5^\circ \tan 15^\circ \tan 45^\circ \tan 75^\circ \tan 85^\circ}$

19. Express $\sin 81^\circ + \tan 71^\circ$ in terms of trigonometric ratios of angles between 0° and 45° .

20. Express $\cos 75^\circ + \cot 75^\circ$ in terms of trigonometric ratios of angles between 0° and 45° .

21. If $\tan 2\theta = \cot(\theta + 6^\circ)$, where 2θ and $\theta + 6^\circ$ are acute angles, find the value of θ .

22. If A and B are acute angles and $\sin A = \cos B$, Prove that $A + B = 90^\circ$.

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23. If A, B, C are the interior angles of a triangle ABC, show that show

that $\sin \frac{B+C}{2} = \cos \frac{A}{2}$

24. $\frac{\cos(90^\circ - \theta)}{\sin \theta} + \frac{\sin \theta}{\cos(90^\circ - \theta)} = 2, \theta \neq 0^\circ$

25. $\cos(81^\circ + \theta) = \sin(9^\circ - \theta)$

26. $\sin(90^\circ - \theta) \cdot \cos(90^\circ - \theta) = \frac{\tan \theta}{1 + \tan^2 \theta}$ **Answers**

| | | | |
|----------------|-------|------------------------------------|-------------------------------------|
| 1. 0 | 2. 2 | 3. 2 | 4. 0 |
| 5. 0 | 6. 0 | 7. 1/2 | 8. 1 |
| 9. 1 | 10. 1 | 11. $\sqrt{3}$ | 12. $\frac{1}{\sqrt{3}}$ |
| 13. 0 | 14. 2 | 15. 1 | 16. 2 |
| 17. 2 | 18. 2 | 19. $\cos 9^\circ + \cot 19^\circ$ | 20. $\sin 15^\circ + \tan 15^\circ$ |
| 21. 28° | | | |