

# JSUNIL TUTORIAL

ACBSE Coaching for Mathematics and Science

(1) A person observes smoke from a cannon when it was fired. 1.5 seconds later, he hears the bang. If the cannon is 510 m away from the observer, calculate velocity of the sound in air.

**Solution:**

**Data:** Distance =  $d = 510$  m, time =  $t = 1.5$  seconds.

**To find:** Velocity of sound

$$\text{Velocity} = \frac{\text{Distance}}{\text{Time}} \quad (\text{Relationship for velocity})$$

$$\therefore v = \frac{510}{1.5} = 340 \text{ m/s}$$

**Ans.** The velocity of the sound in air was 340 m/s.

(2) Using the SONAR, sound pulses are emitted at the surface of the water. The echo is heard after 3 seconds. Find the depth of the sea at that place if velocity of sound in seawater = 1550 m/s.

**Solution:**

**Data:** Velocity of sound in seawater = 1550 m/s. Total time taken by the pulse to leave the transmitter and get reflected from the seabed = 3 seconds (for two way journey)

$$\therefore \text{Time taken by the pulse for 1 way journey} = \frac{3}{2} = 1.5 \text{ s.}$$

**To find:** Depth of the sea i.e. distance.

$$\text{Velocity} = \frac{\text{Distance}}{\text{Time}} \quad (\text{Relationship for velocity})$$

$$\therefore \text{Distance} = \text{Velocity} \times \text{Time}$$

$$\therefore \text{Distance} = 1550 \times 1.5 = 2,325 \text{ m}$$

**Ans.** The depth of the sea at that place = 2,325 m.

\* (3) A person standing before a cliff shouts and hears the echo after 1.6 seconds. If the speed of sound in air is 340 m/s, state the distance between the person and the cliff.

**Solution:**

**Data:** Speed of the sound = 340 m/s. Time for the echo to be heard = 1.6 second. Time for 1 way journey of the

$$\text{sound} = \frac{1.6}{2} = 0.8 \text{ s.}$$

**To find:** Distance between the person and the cliff.

$$\text{Velocity} = \frac{\text{Distance}}{\text{Time}} \quad (\text{Relationship for velocity})$$

$$\therefore \text{Distance} = \text{Velocity} \times \text{Time}$$

$$\therefore \text{Distance} = \text{Speed} \times \text{Time}$$

$$\therefore \text{Distance} = 340 \times 0.8$$

$$\therefore \text{Distance} = 272 \text{ m}$$

**Ans.** The distance between the person and the cliff = 272 m.

(4) A person hears the thunder 3 seconds after a flash of lightning is seen. At what distance has the lightning struck? (Velocity of sound in air = 340 m/s).

**Solution:**

**Data:** Time = 3 s, velocity of sound = 340 m/s.

**To find:** Distance.

$$\text{Velocity} = \frac{\text{Distance}}{\text{Time}} \quad (\text{Relationship for velocity})$$

$$\therefore \text{Distance} = \text{Velocity} \times \text{Time}$$

$$\therefore \text{Distance} = 340 \times 3$$

$$\therefore \text{Distance} = 1020 \text{ m}$$

**Ans.** The lightning struck at a distance of 1020 m.

\* (5) Velocity of sound in air at 0 °C is 332 m/s. It increases by 0.6 m/s for each degree Celsius rise in temperature. At what temperature of air will the velocity be 350 m/s.?

**Solution:**

**Data:** Let the temperature of air be  $t$  °C

Velocity of sound in air at  $t$  °C = 350 m/s

Velocity of sound in air at 0 °C = 332 m/s

$$\therefore \text{The difference between the two velocities} = 350 \text{ m/s} - 332 \text{ m/s} = 18 \text{ m/s.}$$

$$\therefore \text{For an increase of velocity of 0.6 m/s temperature increases by } 1 \text{ } ^\circ\text{C.}$$

$$\therefore \text{For an increase of velocity of 18 m/s, temperature increases by } \frac{18}{0.6} = 30 \text{ } ^\circ\text{C.}$$

$$\therefore \text{The final temperature} = \text{Initial temperature} + \text{increase in temperature}$$

$$\therefore \text{The final temperature} = (0 + 30) \text{ } ^\circ\text{C}$$

$$\therefore \text{The final temperature} = 30 \text{ } ^\circ\text{C}$$

**Ans.** The temperature of air, when the velocity of sound is 350 m/s is 30 °C.

(6) A person observes the smoke from a gun 0.7 second before he hears its bang. If the person is 238 m away from the gun, find the speed of sound in air.

**Solution:**

**Data:** Distance = 238 m, time = 0.7 s.

**To find:** Speed of the sound in air.

$$\text{Speed} = \frac{\text{Distance}}{\text{time}} = \frac{238}{0.7} = 340 \text{ m/s}$$

**Ans.** Speed of sound in air = 340 m/s.

# JSUNIL TUTORIAL

ACBSE Coaching for Mathematics and Science

(7) A person, standing 204 m away from a mountain, fires a gun. Find after how many seconds he hears an echo of the gunfire if the speed of sound in air is 340 m/s.

**Solution:**

**Data:** Speed = 340 m/s, Distance between the person and the mountain is 204 m. There is an echo, hence the sound travels from the gun to mountain and back to the person.

$$\therefore \text{Total distance covered by the sound} = (204 \times 2) \text{ m} = 408 \text{ m.}$$

**To find:** Time taken for the echo to be heard.

$$\text{Speed} = \frac{\text{Distance}}{\text{Time}}$$

$$\text{Time} = \frac{\text{Distance}}{\text{Speed}} = \frac{408}{340} = 1.2 \text{ seconds}$$

**Ans.** The person hears the first echo 1.2 seconds after the gun was fired.

(8) Velocity of sound in air at 0 °C is 332 m/s. at 'ordinary temperature' is 340 m/s. Calculate the 'ordinary temperature' in terms of °C.

**Solution:**

**Data:** Velocity of sound in air at 0 °C = 332 m/s.

Velocity at 'ordinary temperature' = 340 m/s.

$$\therefore \text{Rise in velocity of sound in air} = 340 \text{ m/s} - 332 \text{ m/s} = 8 \text{ m/s.}$$

The velocity increases by about 0.6 m/s for each degree Celsius rise in temperature of air.

$$\therefore \text{Rise in temperature of air} = \frac{8}{0.6} = 13.\bar{3} \text{ }^\circ\text{C}$$

$$\therefore \text{Temperature of air when the velocity of sound is } 340 \text{ m/s} = 0 + 13.\bar{3} \text{ }^\circ\text{C} = 13.\bar{3} \text{ }^\circ\text{C}$$

**Ans.** The word ordinary temperature in this context means a temperature of 13. $\bar{3}$  °C.

(9) Velocity of sound in air at 0 °C is 332 m/s and at room temperature it is 344 m/s. Find the room temperature in terms of degree Celsius.

**Solution:**

**Data:** Velocity of sound in air at 0 °C = 332 m/s.

Velocity at 'room temperature' = 344 m/s

$$\therefore \text{Rise in velocity of the sound in air} = 344 \text{ m/s} - 332 \text{ m/s} = 12 \text{ m/s.}$$

The velocity of sound increases by about 0.6 m/s for each degree Celsius rise in temperature of air.

$$\therefore \text{Rise in Temperature of air} = \frac{12}{0.6} = 20 \text{ }^\circ\text{C.}$$

$$\therefore \text{The temperature when velocity of sound in air} = 344 \text{ m/s} = 0 + 20 \text{ }^\circ\text{C} = 20 \text{ }^\circ\text{C}$$

**Ans.** Room temperature = 20 °C.

(10) Two soldiers A and B are standing on two hill tops C and D respectively which are 760 m apart. Wind is blowing from C to D at a velocity of 144 km/hr. The soldiers fire their guns one after the other. Soldier B fires his gun 5 minutes after soldier A fires his gun. How much time will it take for sound of the gun fire to reach from A to B and from B to A. (Take velocity of sound in still air to be 340 m/s.)

**Solution:**

$$\begin{aligned} \text{Wind velocity} &= 144 \text{ km/hr} \\ &= 144 \times \frac{1000}{60 \times 60} \text{ m/s} \\ &= 40 \text{ m/s} \dots (I) \end{aligned}$$

Wind blows from C to D, soldier A is at C and soldier B is at D.

Velocity of sound when it travels from A to B is 340 m + 40 m = 380 m/s

$$\text{Velocity} = \frac{\text{Distance}}{\text{Time}} \quad (\text{Relationship for velocity})$$

$$\text{Time} = \frac{\text{Distance}}{\text{Speed}} = \frac{760}{380} = 2 \text{ seconds.}$$

Velocity of sound when it travels from B to A is 340 m - 40 m = 300 m/s

$$\text{Time} = \frac{\text{Distance}}{\text{Velocity}} = \frac{760}{300} = 2.53 \text{ seconds.}$$

**Ans. (i)** It takes 2 seconds for the sound to reach from A to B.

**(ii)** It takes about 2.53 seconds for the sound to reach from B to A.

(11) A person stands between two cliffs and fires a gun. He hears two successive echoes in 2 seconds and 5 seconds after the gun was fired. Find the distance between the two cliffs.

**Solution:**

Let the distance between the person and the nearest cliff = (x) m and let the distance between the person and

distant cliff = (y) m.

$$\therefore \text{The distance between two cliffs} = (x + y) \text{ m} \dots (I)$$

First echo was heard 2 s after the gun was fired.

Total distance covered by the sound to produce the first echo = (x + x) = (2x) m

Time required to cover (2x) m (i.e. two way journey) = 2 s

$$\therefore \text{Time required to cover (x) m (i.e. one way journey)}$$

$$= \frac{2}{2} = 1 \text{ s}$$

$$\text{Velocity} = \frac{\text{Distance}}{\text{Time}} \quad (\text{Relationship for velocity})$$

# JSUNIL TUTORIAL

ACBSE Coaching for Mathematics and Science

- ∴ Distance = Velocity × Time
- ∴ Distance (x) = 340 × 1 = 340 m.  
The second echo, produced by the distant cliff was heard after 5 s.  
The total distance covered by the sound to produce this echo = (2y) m.
- ∴ Time taken by the sound to complete one-way journey
- $$= \frac{5}{2} = 2.5 \text{ s.}$$
- ∴ Distance covered by the sound during 1 way journey
- $$= \text{Velocity} \times \text{Time}$$
- $$= 340 \times 2.5 = 850 \text{ m.}$$
- ∴ Distance (y) = 850 m
- ∴ Distance x + y = (340 + 850) m = 1190 m = 1.19 km

**Ans.** The distance between the two cliffs is 1190 m or 1.19 km.

**(12)** A boat equipped with SONAR is sailing in a fresh water lake. It emits a sharp pulse of sound, which is reflected from the bottom of the lake after 0.5 s. Determine the depth of the lake at that spot.

**Solution:**

Velocity of sound in fresh water is 1410 m/s. The time taken for sound to be reflected from the lake bottom (i.e. after two way journey) = 0.5 s

$$\therefore \text{Time required for 1 way journey} = \frac{0.5}{2} = 0.25 \text{ s}$$

$$\text{Velocity} = \frac{\text{Distance}}{\text{Time}} \quad (\text{Relationship for velocity})$$

$$\therefore \text{Distance} = \text{Velocity} \times \text{Time}$$

$$\therefore \text{Distance} = 1410 \times 0.25$$

$$\therefore \text{Distance} = 352.5 \text{ m}$$

**Ans.** The distance between the boat and the bottom of the lake i.e. depth of the lake is 352.5 m.

**13.** Calculate the wavelength of a sound wave whose frequency is 220 Hz and speed is 440 m/s in a given medium. (Textbook question)

**SOLUTION** Velocity of the sound wave ( $v$ ) = 440 m/s

Frequency ( $\nu$ ) of the sound wave = 220 Hz

Wavelength of the sound wave ( $\lambda$ ) = ?  
(to be calculated)

We know,  $v = \nu \times \lambda$

$$440 \text{ m/s} = 220 \text{ Hz} \times \lambda$$

or  $\lambda = \frac{440 \text{ m/s}}{220 \text{ Hz}}$

$$\lambda = 2 \text{ m}$$

So, the wavelength of the sound wave is 2 m.

**14.** A source produces 15 waves in 3 seconds. The distance between a crest and a trough is 15 cm. Find the (a) frequency (b) wavelength, and (c) velocity of the wave.

**SOLUTION** (a) Number of waves produced in 3 seconds

$$= 15$$

∴ Number of waves produced in 1 second

$$= \frac{15}{3} = 5$$

So, the frequency ( $\nu$ ) of this wave is 5 Hz.

(b) Distance between crest and trough

$$= 15 \text{ cm} = \text{half the wavelength}$$

$$\text{So, } \lambda = 15 \times 2 \text{ cm}$$

$$= 30 \text{ cm} = \frac{30}{100} \text{ m} = 0.3 \text{ m}$$

Thus, the wavelength of the wave is 30 cm or 0.3 m.

(c) We know,

$$v = \nu \times \lambda$$

$$v = 5 \text{ Hz} \times 0.3 \text{ m}$$

$$v = 1.5 \text{ m/s}$$

Thus, the velocity of the wave is 1.5 m/s.

**15.** A body vibrating with a time period of 2 milliseconds produces a wave travelling in a medium with a velocity of 1250 m/s. What is the wavelength?

**SOLUTION** Time period ( $T$ ) = 2 milliseconds

$$= \frac{2}{1000} \text{ seconds}$$

$$\text{Velocity } (v) = 1250 \text{ m/s}$$

$$\text{Wavelength } (\lambda) = ?$$

We know,  $v = \nu \times \lambda$

$$v = \frac{1}{T} \times \lambda \quad [\text{since } \nu = \frac{1}{T}]$$

$$1250 \text{ m/s} = \frac{1}{\frac{2}{1000} \text{ s}} \times \lambda$$

$$1250 \text{ m/s} = \frac{1000}{2} \text{ s} \times \lambda$$

$$\lambda = 1250 \text{ m/s} \times \frac{2}{1000} \text{ s}$$

$$= 2.5 \text{ m}$$

Thus, the wavelength of wave is 2.5 m.