

# CITY CENTRAL HIGH SCHOOL

## CLASS 9<sup>th</sup> ANNUAL EXAMINATION

(2019-20)

### SUBJECT – MATHEMATICS

Time: 3 Hrs.

M.M. 80

#### General Instruction:

1. All questions are compulsory.
2. The paper consists of 40 questions divided into four sections A, B, C and D. Section A comprises of 20 questions of 1 marks each. Section B comprises of 6 question of 2 marks each. Section C comprises of 8 questions of 3 marks each. Section D comprises of 6 question of 4 marks each.
3. There is no over all choice in this question paper. All though internal choices has been provided in some question.

#### SECTION - A

1.  $\sqrt[4]{\sqrt[3]{2^2}}$

a)  $2^{\frac{-1}{6}}$   
c)  $2^{\frac{1}{6}}$

b)  $2^{-6}$   
d)  $2^6$

or

$(625)^{0.16} \times (625)^{0.09} = ?$

a) 5  
c) 125

b) 25  
d) 625.25

2. If  $\frac{x}{y} + \frac{y}{x} = -1$  ( $x, y \neq 0$ ), the value of  $x^3 - y^3$  is

a) -1

b) 1

c) 0

d)  $\frac{1}{2}$

3. If  $a + b + c = 0$  then  $\frac{a^2}{bc} + \frac{b^2}{ca} + \frac{c^2}{ab} = ?$

a) 1

b) 0

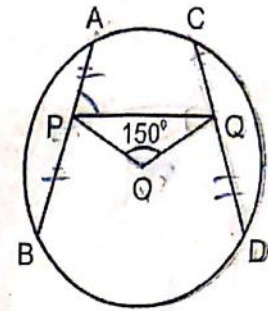
c) -1

d) 3

4. ✓ The values of  $249^2 - 248^2$  is
- |          |        |
|----------|--------|
| a) $1^2$ | b) 477 |
| c) 487   | d) 497 |
5. ✓ If  $(2, 0)$  is a solution of the linear equation  $2x + 3y = K$ , then the value of  $K$  is
- |      |      |
|------|------|
| a) 4 | b) 6 |
| c) 5 | d) 2 |
6. ✓ How many linear equations in  $x$  and  $y$  can be satisfied by  $x = 1$  and  $y = 2$ ?
- |                    |          |
|--------------------|----------|
| a) Only One        | b) Two   |
| c) Infinitely many | d) Three |
7. The point whose ordinate is 4 and which lies on  $y$ -axis is
- |             |             |
|-------------|-------------|
| a) $(4, 0)$ | b) $(0, 4)$ |
| c) $(1, 4)$ | d) $(4, 2)$ |
- or
- If  $P(-1, 1)$ ,  $Q(3, -4)$ ,  $R(1, -1)$ ,  $S(-2, -3)$  and  $T(-4, 4)$  are plotted on the graph paper, then the points in the fourth quadrant are
- |            |            |
|------------|------------|
| a) P and T | b) Q and R |
| c) Only S  | d) P and R |
8. The angles of a triangle are in the ratio  $2 : 4 : 3$ . The smallest angle of the triangle is
- |               |               |
|---------------|---------------|
| a) $60^\circ$ | b) $40^\circ$ |
| c) $80^\circ$ | d) $20^\circ$ |
9. Two sides of a triangle are of length  $5\text{cm}$  and  $1.5\text{cm}$ . The length of the third side of the triangle cannot be.
- |                   |                   |
|-------------------|-------------------|
| a) $3.4\text{cm}$ | b) $3.6\text{cm}$ |
| c) $3.8\text{cm}$ | d) $4.1\text{cm}$ |
- 5

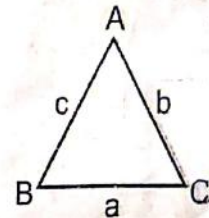
10. The figure obtained by joining the mid point of the sides of a rhombus, taken in order is
- a) a rhombus
  - b) a rectangle
  - c) a square
  - d) any Parallelogram

11. In Fig. AB and CD are two equal chords of a circle with centre O. OP and OQ are perpendiculars on chords AB and CD respectively. If  $\angle POQ = 150^\circ$ , then  $\angle APQ$  is equal to



- a)  $30^\circ$
- b)  $75^\circ$
- c)  $15^\circ$
- d)  $60^\circ$

12. By the Heron's formula, the area of  $\Delta ABC$  is given by  $\Delta =$  \_\_\_\_\_ sq. unit.



13. The sides of a triangle are 56cm, 60cm, and 52cm long. Then the area of the triangle is

- a)  $1322\text{cm}^2$
- b)  $1311\text{cm}^2$
- c)  $1344\text{cm}^2$
- d)  $1392\text{cm}^2$

14. The sides of a triangle are in the ratio 5:12:13 and its perimeter is 150cm. The area of the triangle is

- a)  $375\text{cm}^2$
- b)  $750\text{cm}^2$
- c)  $250\text{cm}^2$
- d)  $500\text{cm}^2$

15. The total surface area of a cone whose radius is  $\frac{r}{2}$  and short height  $2l$  is

- a)  $2\pi r (l + r)$
- b)  $\pi r (l + \frac{r}{4})$
- c)  $\pi r (l + r)$
- d)  $2\pi r l$

16. The radius of a hemispherical balloon increases from 6cm to 12cm as air is being pumped into it. the ratios of the surface areas of the

balloon in the two cases is

- a) 1 : 4                                      b) 1 : 3  
c) 2 : 3                                      d) 2 : 1

17. The class mark of the class 90 – 120 is :

- a) 90    b) 105  
c) 115    d) 120

18. The mean of five number is 30. If one number is excluded their mean becomes 28. The excluded number is :

- a) 28    b) 30  
c) 35    d) 38

19. A coin is tossed 60 times and the tail appears 35 times. What is the probability of getting a head ?

- a)  $\frac{7}{12}$     b)  $\frac{12}{7}$   
c)  $\frac{5}{12}$     d)  $\frac{12}{5}$

20. Fill in the blanks :

If E be an event, then  $P(E) + P(\text{not } E) = \underline{\quad 1 \quad}$

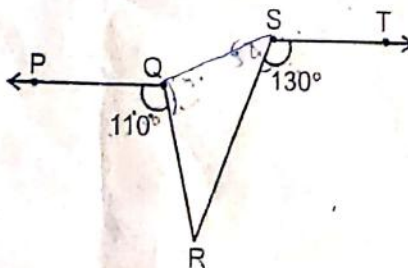
### SECTION - B

21. If the point (3, 4) lies on the graph of  $3y = ax + 7$ , then find the value of a.

or

Find four different solutions of  $2x + y = 6$ .

22. If  $PQ \parallel ST$ ,  $\angle PQR = 110^\circ$  and  $\angle RST = 130^\circ$ , find  $\angle QRS$



23. Find the area of the trapezium whose parallel sides are 14cm and 10cm and whose height is 6cm.
24. The perimeter of a an isosceles triangle is 32cm. The ratio of the equal side to its base is 3:2. Find the area of the triangle.
25. The diameter of a roller is 84cm and its length is 120cm. It takes 500 complete revolutions to move once cover to level a playground. Find the area of the playground in  $m^2$ .
26. A die was rolled 100 times and the number of times 6 appeared was noted. If the probability of getting a 6 be  $\frac{2}{5}$ , how many times did 6 come up?

or

1500 families with 2 children each, were selected randomly and the following data were recorded.

Number of girls in a family	2	1	0
Number of families	102	675	723

out of these families, one family is selected at random. What is the probability that the selected family has.

- i) 2 girls  
ii) 1 girl

### SECTION - C

27. If  $a = 2 + \sqrt{3}$ , then find the value of  $a - \frac{1}{a}$ .

28. Factorise:  $a(a-1) - b(b-1)$

or

If  $P = 2 - a$ , prove that  $a^2 + 6ap + p^3 - 8 = 0$

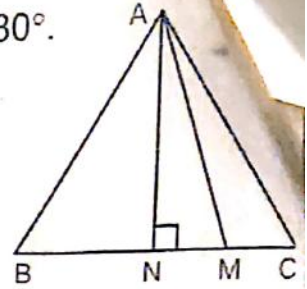
29. The taxi fare in a city as follows : for the first kilometre, the fare is ₹ 25 and for the subsequent distance it is ₹ 14 per km. Taking the distance covered as  $x$  km and total fare as ₹ $y$ , write the linear equation for this information and draw its graph.

30. Three vertices of a rectangle are  $(3, 2)$ ,  $(-4, 2)$  and  $(-4, 5)$ , plot these points on a graph paper and the coordinates of the fourth vertex.

31. Prove that the sum of three angles of a triangle is  $180^\circ$ .

or

In a  $\triangle ABC$ ,  $\angle B > \angle C$  if  $AM$  is the bisector of  $\angle ABC$  and  $AN \perp BC$ . Prove that  $\angle MAN = \frac{1}{2}(\angle B - \angle C)$



32. The measure of angles of a quadrilateral are  $(x+20)^\circ$ ,  $(x-20)^\circ$ ,  $(2x+5)^\circ$  &  $(2x-5)^\circ$ . Find the value of  $x$ .

or

$E$  is the mid point of the median  $AD$  of  $\triangle ABC$  and  $BE$  is produced to meet  $AC$  at  $F$ . Show that  $AF = \frac{1}{3} AC$ .

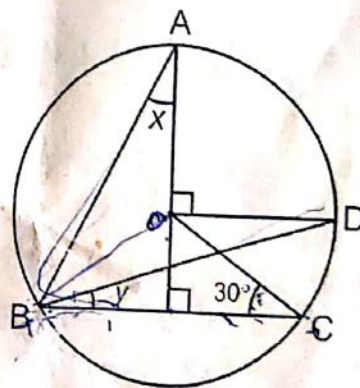
33. Prove that parallelogram on the same base and between the same parallels are equal in area.

or

$ABCD$  is trapezium in which  $AB \parallel DC$ ,  $DC = 30\text{cm}$  and  $AB = 50\text{cm}$ . If  $x$  and  $y$  are, respectively the mid points of  $AD$  and  $BC$  prove that

$$\text{ar}(\text{DCYX}) = \frac{7}{9} \text{ar}(\text{XYBA})$$

34. In figure,  $O$  is the centre of the circle.  $\angle BCO = 30^\circ$ . Find  $x$  and  $y$ .



### SECTION - D

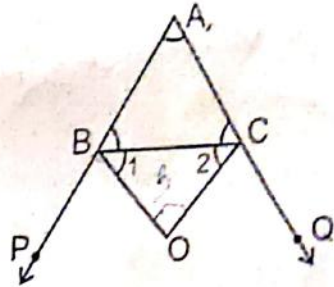
35. Show that :

$$\frac{1}{(3 - \sqrt{8})} - \frac{1}{(\sqrt{8} - \sqrt{7})} + \frac{1}{(\sqrt{7} - \sqrt{6})} - \frac{1}{(\sqrt{6} - \sqrt{5})} + \frac{1}{(\sqrt{5} - 2)} = 5$$

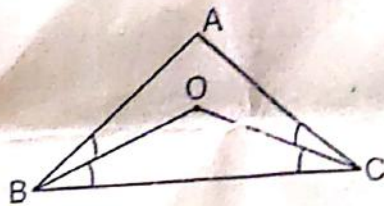
36. Factorise the expression  
 $8x^3 + 27y^3 + 36x^2y + 54xy^2$

37. In a  $\triangle ABC$ .

i) The sides AB and AC are produced to P and Q respectively. If the bisectors of  $\angle PBC$  and  $\angle QCB$  intersect at a point O. Prove that  $\angle BOC = 90^\circ - \frac{1}{2}\angle A$



ii) The bisectors of  $\angle B$  and  $\angle C$  intersect each other at a point O. Prove that  $\angle BOC = 90^\circ + \frac{1}{2}\angle A$



or

If the bisector of an angle of a triangle also bisect the opposite side. Prove that the triangle is isosceles.

38. Construct a triangle XYZ in which  $\angle Y = 30^\circ$ ,  $\angle Z = 90^\circ$  and  $XY + YZ + ZX = 11\text{cm}$ . Write steps of construction also.

39. The radius of a sphere is increased by 10%. Prove that the volume will be increased by 33.1% approximately.

or

The ratio of the curved surface area and the total surface area of a circular cylinder is 1:2 and the total surface area is  $616\text{cm}^2$ . Find its volume

40. The mean marks (out of 100) of boys and girls in an examination are 70 and 73 respectively. If the mean marks of all the students in the examination is 71. Find the ratio of the number of boys to the number of girls.

or

The mean of 100 items was found to be 64. Later on it was discovered that two items misread as 26 and 9 instead of 36 and 90 respectively. Find the correct mean.