

CLASS: X

1. If $\cot\theta = 15/8$, evaluate $\frac{(2 + 2\sin\theta)(1 - \sin\theta)}{(1 + \cos\theta)(2 - 2\cos\theta)}$ (225/64)
2. If $7\sin^2\theta + 3\cos^2\theta = 4$, show that $\tan\theta = 1/\sqrt{3}$
3. Evaluate: $\tan^2 60^\circ - 2\cos^2 60^\circ - \frac{3}{4}\sin^2 45^\circ - 4\sin^2 30^\circ$ (9/8)
4. Evaluate: $\frac{\sec^2 54^\circ - \cot^2 36^\circ}{\operatorname{Cosec}^2 57^\circ - \tan^2 33^\circ} + 2\sin^2 38^\circ \sec^2 52^\circ - \sin^2 45^\circ$ (5/2)
5. Evaluate: $\sqrt{2}\tan^2 45^\circ + \cos^2 30^\circ - \sin^2 60^\circ$ ($\sqrt{2}$)
6. If $\sec^2\theta (1 + \sin\theta)(1 - \sin\theta) = k$, find the value of k ($k = 1$)
7. Evaluate: $(\sin 90^\circ + \cos 45^\circ + \cos 60^\circ)(\cos 0^\circ - \sin 45^\circ + \sin 30^\circ)$ (7/4)
8. Find the value of:

$$\frac{2\sin 68^\circ}{\cos 22^\circ} \cdot \frac{2\cot 15^\circ}{5\tan 75^\circ} \cdot \frac{3\tan 45^\circ \tan 20^\circ \tan 40^\circ \tan 50^\circ \tan 70^\circ}{5}$$
 (1)
9. If $\sin(A + B) = 1$, $\cos(A - B) = 1$, find A and B ($45^\circ, 45^\circ$)
10. If $\cos(40^\circ + x) = \sin 30^\circ$, find the value of x (20°)
11. $\sin 4A = \cos(A - 20^\circ)$, where $4A$ is an acute angle, find the value of A (22°)
12. Find the acute angles A and B , $A > B$, if $\sin(A + 2B) = \sqrt{3}/2$ and $\cos(A + 4B) = 0$ ($30^\circ, 15^\circ$)
13. Evaluate: $\sec(90 - \theta)\operatorname{cosec}\theta - \tan(90 - \theta)\cot\theta + \frac{\cos^2 35^\circ + \cos^2 55^\circ}{\tan 5^\circ \tan 15^\circ \tan 45^\circ \tan 75^\circ \tan 85^\circ}$ (2)
14. If $\sin A - \cos B = 0$, prove that $A + B = 90^\circ$
15. If $\frac{\sin\theta + \cos\theta}{\sin\theta - \cos\theta} = \frac{5}{3}$, evaluate $\frac{7\tan\theta + 2}{2\tan\theta + 7}$ (2)
16. What is the maximum value of $1/\sec\theta$
17. If A, B and C are interior angles of triangle ABC , show that $\cos\left\{\frac{B+C}{2}\right\} = \frac{\sin A}{2}$
18. If $x = a\sin\theta$, $y = b\tan\theta$. Prove that $\frac{a^2}{x^2} - \frac{b^2}{y^2} = 1$
19. Prove that: $\frac{1}{1 + \sin\theta} + \frac{1}{1 - \sin\theta} = 2\sec^2\theta$
20. Prove that: $\frac{\sin\theta}{1 + \cos\theta} + \frac{1 + \cos\theta}{\sin\theta} = 2\operatorname{cosec}\theta$