

SUMMATIVE ASSESSMENT - I, 2016-17 MATHEMATICS Class - X

QVHDP01

Maximum Marks: 90

Time Allowed: 3 hours

- X and Y are points on the sides AB and AC respectively of a triangle ABC such that $\frac{AX}{AB} = \frac{1}{4}$, AY = 2 cm and YC = 6 cm. Find whether XY || BC or not.
- Evaluate $\frac{\operatorname{cosec} 13^\circ}{\operatorname{Sec} 77^\circ} = \frac{\cot 20^\circ}{\tan 70^\circ}$
- If $x = 3 \sin \theta$ and $y = 4 \cos \theta$, find the value of $\sqrt{16x^2 + 9y^2}$
- If the median of the series exceeds the mean by 3, find by what number the mode exceeds its mean.

SECTION - B

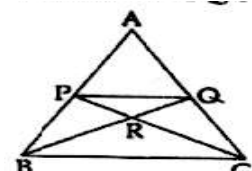
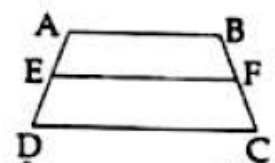
- Check whether 4^n can end with the digit 0 for any natural number n.
- Find the prime factorisation of the denominator of the rational number equivalent to 8.39.
- Given the linear equation $3x - 4y = 9$ write another linear equation in these two variables such that the geometrical representation of the pair so formed is (i) intersecting lines (ii) coincident lines
- In a rectangle ABCD, E is the middle point of AD. If AD = 40 m and AB = 48 m, then find EB
- If $\sin(A + B) = 1$ and $\sin(A - B) = \frac{1}{2}$, then find A and B.
- The following table shows the daily Consumption of milk in an houses of a locality

Consumption (in litres)	0 - 0.5	0.5 - 1	1 - 1.5	1.5 - 2	2 - 2.5
Number of houses	7	15	10	5	3

Find the modal class and media class for the data.

SECTION - C

- Find the HCF of 1620, 1723 and 255 by Euclid's Division algorithm.
- On dividing the polynomial $4x^4 - 5x^3 - 39x^2 - 46x - 2$ by the polynomial $g(x)$. the quotient and remainder were $x^2 - 3x - 5$ and $-5x + 8$ respectively. Find $g(x)$
- If α and β are zeroes of a polynomial $x^2 + 6x + 9$, then form a polynomial whose zeroes are $-\alpha$ and $-\beta$
- Solve the following pair of equations: $49x + 51y = 499$ and $51x + 49y = 501$
- In the figure, if $EF \parallel DC \parallel AB$, then prove that $AE/ED = BF/FC$
- In the given figure, $\triangle ABC$, $PQ \parallel BC$ and $BC = 3PQ$. Find the ratio of the area of $\triangle PRQ$ and area $\triangle CRB$ where PC and BQ intersect at R.
- Given a right angled $\triangle ABC$, right angled at B. In which $\tan A = \frac{15}{8}$ and $\tan C = \frac{8}{15}$, then find the value of $\sin A \cdot \cos C + \cos A \cdot \sin C$



18. Prove that: $(\operatorname{cosec}\theta - \sin\theta)(\sec\theta - \cos\theta) = \sin\theta \cos\theta = \frac{1}{\tan\theta + \cot\theta}$ 19. In a school IQ of students of Class X are given in the following frequency distribution:

IQ	120-130	130-140	140-150	150-160	160 - 170
Number of students	10	80	100	50	10

Find the mean IQ of students.

20. An NGO working for welfare of cancer patients, maintained its records as follows: Find mode.

Age of patients (in years)	0-20	20-40	40-60	60-80
Number of patients	35	315	120	50

SECTION-D

21. Prove that only one of the number $n - 1$, $n + 1$ or $n + 3$ is divisible by 3 where n is any positive integer. Explain,

22. Obtain all other zeroes of the polynomial $x^4 + x^3 - 16x^2 - 4x + 48$. If two of its zeroes are 2 and -4

23. Solve the following pair of linear equations graphically $6x - y + 4 = 0$ and $2x - 5y = 8$. Shade the region bounded by the lines and y-axis.

24. Raghav scored 70 marks in a test, getting 4 marks for each right answer and losing 1 mark for each wrong answer. Had 5 marks been awarded for each correct answer and 2 marks been deducted for each wrong answer, then Raghav would have scored 80 marks. How many questions he attempted.

Which value would Raghav violate if he resorts to unfair means?

25. On three line segments OA, OB and OC there are points L, M and N respectively such that $LM \parallel AB$ and $MN \parallel BC$. If L, M, N and A, B, C are non-collinear points, then prove that $LN \parallel AC$.

26. Two poles of height 'p' and 'q' metres are standing vertically on a level ground, 'a' metres apart. Prove that the height of the point of intersection of the lines joining the top of each pole to the foot of the opposite pole is given by $\frac{pq}{p+q}$

27. if $\theta = 45^\circ$ then verify the following (i) $\sin 2\theta = 2 \sin\theta \cos\theta$ (ii) $\cos 2\theta = \cos^2\theta - \sin^2\theta$.

28. If $\tan A + \sin A = m$ and $\tan A - \sin A = n$, then prove that $(m^2 - n^2)^2 = 16 mn$.

29. If $\sec\theta - \tan\theta = x$, show that: $\sec\theta = \frac{1}{2} \left(x + \frac{1}{x} \right)$ and $\tan\theta = \frac{1}{2} \left(x - \frac{1}{x} \right)$

30. Production yield per hectare of wheat of some farms of a village are given in the following table

Production (kg/ha)	40- 45	45 - 55	55 - 60	60 - 65	65 - 70	70- 75	75-80	80 - 85	
Number of farms	1	9	15	18	40	26	16	14	10

Draw a 'less than type' ogive and 'more than type' ogive for this data

31. Find the missing frequencies and the median for the following distribution if the mean is 1.46

No. of accidents	0	1	2	3	4	5	Total
No. of days	46	x	y	25	10	5	200